Study of Multiplexing for Group-based Quality of Service Delivery *

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Abstract

In this work, the problem of scheduling packets with a group as opposed to an individual deadline is considered. Packets of the same group are supposed to belong in the same application data unit for which a deadline is set, and they are assumed to arrive over fixed time intervals (frames). The Frame-based Shortest Time to Extinction (F-STE) scheduling policy is considered at a multiplexer fed by multiple streams with group deadlines. The performance of the F-STE policy is evaluated in terms of the induced packet loss (deadline violation) probabilities. It is established that the F-STE policy outperforms the First In First Out (FIFO) policy while the implementation complexity of the former is argued to be similar to that of the latter.

1 Introduction

High speed networks are today considered to be capable of supporting high-rate real-time applications such as video and multimedia. In order for the Quality of Service (QoS) of such applications to be delivered, networks must meet stringent performance requirements in terms of delay, delay jitter, throughput and packet loss. The timely delivery of packets associated with a real time application can be achieved in a number of ways. The direct approach would be to associate deadlines by which the packets must be transmitted and employ deadline-based scheduling mechanisms within the network. Examples of such scheduling policies are the Earliest Due Date (EDD) [8, 9, 10], the Delay-EDD [7] and the Shortest-Time-to-Extinction (STE) [11]. Alternatively, scheduling policies which control the induced delay jitter or guarantee a certain transmission (service) rate could be employed. Such policies include the Virtual Clock (VC) [1, 2], Hierarchical Round Robin (HRR) [5], Stop-and-Go [6], Rate Controlled Static Priority Queueing (RCSP) [16], Fair Queueing [12], Weighted Fair Queueing (WFQ) [15], also known as General Processor Sharing (GPS), and the packet based version of GPS, Packet-by-Packet Generalized Processor Sharing (PGPS) [13, 14]. Since this paper proposes and investigates a new *deadline* driven scheduling policy, the related EDD and STE policies mentioned above are discussed in more detail.

The classical EDD policy minimizes the maximum lateness and maximum tardiness by transmitting packets in the order of their due dates. The lateness of a packet is defined to be the difference between the finishing time of its transmission and its due date. Its tardiness is given by $\max\{0, lateness\}$. The STE policy is very similar to the EDD policy in the sense that the packet with the earliest due date is served first. However, it differs from the EDD in that packets which miss their deadline (expired packets) are not transmitted. It has been established that the STE scheduling policy is optimal in the sense that it maximizes the fraction of packets transmitted before their deadline or, equivalently, minimizes the deadline violation probability.

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In some applications, such as packetized voice or video, packets must be transmitted before their deadlines expire in order to be useful. On the other hand, these applications can tolerate the loss of a small fraction of packets. Clearly, the STE scheduling policy is optimal for such applications. However, implementation of the STE policy requires a time-consuming sorting process in order to identify the task with the earliest deadline. This makes the STE policy too complex for real-time realization in high speed networks. For this reason, the simple to implement FIFO policy is often employed. Although the performance of the FIFO scheduling policy is typically inferior to that of the STE policy with respect to the induced deadline violation probability, it is easy to establish that the STE policy and the FIFO policy that drops expired packets become identical if all packets sharing the same resource have identical time to extinction upon arrival. In such environments, the easy to implement FIFO which drops expired packets is also optimal in the sense that it minimizes the deadline violation probability.

The nature of most real-time applications suggests, however, that a deadline be associated with an application data unit (group of packets), such as a video-frame in video applications, rather than with individual packets. For example, in the VBR video encoder, the data for one horizontal strip of blocks is assembled into a single self-contained unit which is transmitted by means of multiple ATM cells (the unit is referred to as a video packet) [4]. The address of the strip in the frame provides a time reference for decoder synchronization. For such applications, a deadline should be associated with each data unit rather than with each packet. Packets belonging in the same group now have variable times to extinction upon arrival, and the FIFO policy is non-optimal even if all the applications have identical QoS requirements.

In this work, the Shortest Time to Extinction (STE) scheduling policy is considered for scheduling packets with a group as opposed to individual deadline. Packets of the same group are defined here as packets arriving over a fixed time interval (frame). Packets belonging to the group with the earliest deadline (shortest time to extinction) are served first and the policy is called Frame-STE (F-STE) due to the central role of the underlying frame in determining the arrivals and the associated deadlines. It is easy to establish that the F-STE is equivalent to a dynamic Deadline-Ordered Head-of-Line (DO–HoL) priority scheduling policy. Clearly, F-STE is optimal in the sense that it minimizes the deadline violation probability. While a scheduler implementing the STE policy must search for the packet with the shortest time to extinction every time it serves a packet, no such search is necessary for the F-STE policy. This is an advantage intrinsic to group-based scheduling policies, in which the scheduling priority needs to be updated less often than in a packet-based scheduling policy, and has been pointed out by other authors (for example, [3]).

2 Description of the System and the Scheduling Policy

A network node with N incoming and one outgoing links is considered in this paper. All links are assumed to have the same capacity and thus a packet (fixed size information unit) transmission requires the same amount of time, referred to as the slot. Slot level system synchronization is assumed implying that packet arrivals and departures from the node occur at slot boundaries.

In addition to the time slot, a larger time constant of length T (in slots), called frame, is associated with each of the input streams. T takes integer values and is assumed to have the same value for all streams to simplify the analysis and the discussion. The relative shift of the frame boundaries of the incoming streams can be arbitrary. Without loss of generality and for simplicity, the frame boundaries are assumed to be uniformly distributed in this paper. Packet arrivals associated with the same stream and frame occur according to a Bernoulli process with a fixed rate. This rate may be different for different streams.

The frame is also assumed to modulate the QoS of the associated packets. Specifically, all packets of a stream arriving over the same frame are assumed to have the same deadline, set to be equal to the end of the next frame. Since the objective of this work is to determine whether significant performance gain can be achieved under the proposed policy, the deadline is set so that the analysis complexity be minimized. Packets which are not transmitted (served) by their

deadline are dropped.

It is easy to see that packets with the same deadline (end of next frame) will have different times to extinction upon arrival, since their arrival times are different (one packet per slot per frame). When the frame boundaries associated with different streams are not synchronized, which would be typically the case, it is easy to establish that earlier arriving packets from one stream may have a larger time to extinction than later arriving packets from a different stream. As a result, the easy to implement FIFO policy would not serve packets in order of decreasing times to extinction and, for this reason, would not minimize the deadline violation probabilities; as said earlier, these probabilities are minimized under the STE policy.

In this paper, packets are served according to the STE policy. Because of the frame-structured packet arrivals and QoS definition, the STE policy – called in this environment Frame-based STE (F-STE) - is easy to implement, and thus, can be employed in a high-speed networking environment. Details of a simple implementation are presented in the next subsection.

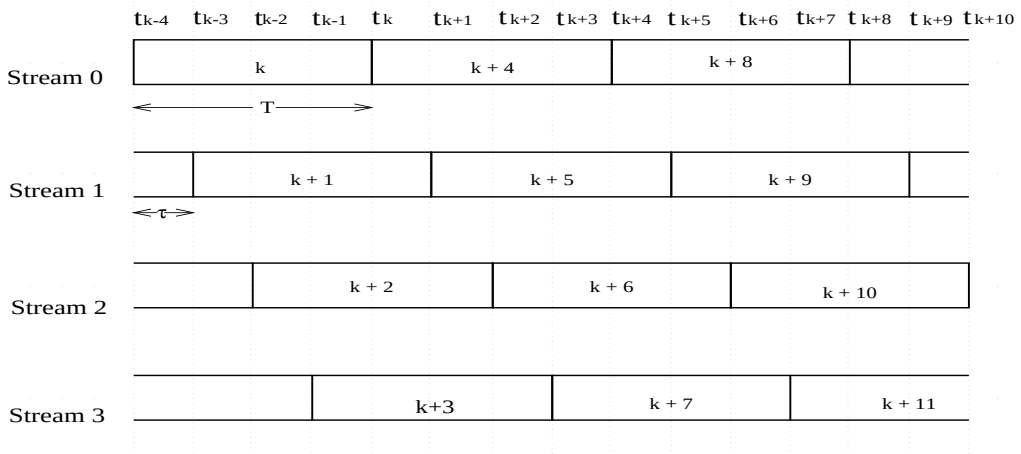

Figure 1: Frame structure of $N = 4$ traffic streams

The following definitions and alternative policy description will be useful in both the analysis and the implementation of the F-STE policy. Figure 1 depicts the arrival axes of $N = 4$ streams. The frames of all streams are identical (of length equal to T slots) and their boundaries are uniformly distributed. Let $\{t_k\}$ denote the sequence of frame boundaries from any streams, that is, t_k denotes the time when the kth frame ends. The deadline of packets associated with the frame ending at t_k is time t_{k+N}. Let I_k denote the stream whose frame ends at t_k; $I_k \epsilon \{0, 1, 2, \ldots, N-1\}$.

According to the F-STE policy and in view of the above assumptions, the scheduler serves the streams according to the ordered HoL priority $(I_{k+1}, I_{k+2}, \ldots, \ I_{k+N})$ over the interval $(t_k, t_{k+1}]$. That is, high priority is given to packets from stream I_{k+1}, second highest priority is given to the packets from stream I_{k+2}, etc. It is easy to see that this policy serves packets in order of decreasing times to extinction. The ordered-HoL priority $(I_{k+1}, I_{k+2}, \ldots, \ I_{k+N})$ is cyclically shifted at the next frame boundary to $(I_{k+2}, I_{k+3}, \ldots, \ I_{k+N+1})$; and for this reason, the comprehensive service policy is called Dynamic-Ordered HoL priority policy (DO-HoL).

2.1 Implementation

The F-STE policy (or DO-HoL policy which drops expired packets) can be implemented without requiring a search for the packet with the shortest time to extinction, as described below and depicted in Figure 2.

Each stream is assigned a logically distinct data queue of capacity T which is the maximum number of packets delivered by the stream over one frame. At time t_k, the content of the data

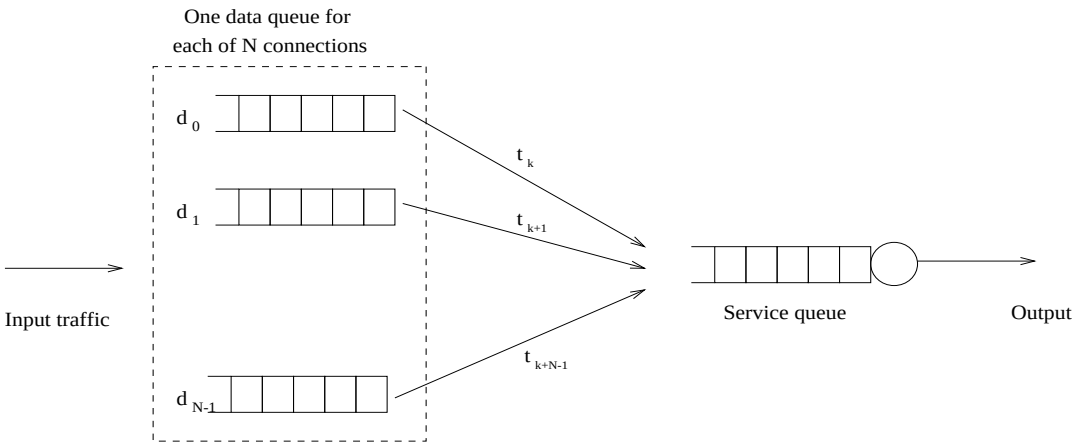

Figure 2: Implementation of the F-STE policy at a node with N incoming links (packets arriving over a frame accumulate in the corresponding data queue and are shifted to the service queue at the end of the frame).

queue I_k is shifted to the service queue of capacity T. If the service queue overflows, the dropped packets will be precisely the ones which will miss their deadline. Packets accepted by the service queue will be served within T time units after their shifting since the service queue is served continuously. If the service queue becomes empty at some time t, $t_k < t < t_{k+1}$, then the server either remains idle until data queue I_{k+1} is shifted into the service queue at t_{k+1} (non-work-conserving F-STE policy), or the server attends to the data queues according to the DO-HoL priority policy (work-conserving F-STE policy).

3 Performance Analysis

In this section, the packet loss (deadline violation) probability is derived for N streams served under the F-STE policy. The arrival process and QoS requirements are as described earlier.

Let τ_k denote the interval (in slots) between the two consecutive frame boundaries ending at t_k and t_{k+1}; that is $\tau_k = t_{k+1} - t_k$. In view of the assumptions in section 2, τ_k is independent of k and will be denoted by τ. Clearly, $\tau = \frac{T}{N}$. Let I_k denote the data queue whose content is to be shifted to the service queue at t_k. Let Q_k denote the service queue occupancy at time t_k, after the packets from data queue I_k are shifted into the service queue. The 2-dimensional process $\{Q_k, I_k\}_{k\geq 0}$ with state space $\{(i,j) : 0 \leq i \leq T, 0 \leq j \leq N-1\}$ is defined to be the *system* process and is employed in the analysis of the scheduling policies. Let $P(i,j,i',j')$ denote the transition probability that process $\{Q_k, I_k\}_{k\geq 0}$ moves from state (i,j) at time t_k to state (i',j') at time t_{k+1}. Note that this probability is zero if $j' \neq (j+1)\mathrm{mod}(N)$, since only transitions from j to $j' = (j+1)\mathrm{mod}(N)$ are possible. Throughout the paper, j' will always be equal to $(j+1)\mathrm{mod}(N)$.

In the next subsection, the system process $\{Q_k, I_k\}_{k\geq 0}$ is determined under the non-work-conserving F-STE policy. In subsection 3.2, certain auxiliary processes are defined in order to obtain bounds or approximations on the evolution of the system process $\{Q_k, I_k\}_{k\geq 0}$ under the work-conserving F-STE policy. By employing the derivations of 3.1 and 3.2, the packet loss (deadline violation) probability is derived for all cases in subsection 3.3. In the derivations that follow, A_m^k denotes the random variable representing the number of packets from stream k arrived over m slots. The probability mass function of A_m^k is given by the convolution of the Bernoulli random variables of the associated stream which are assumed to be of fixed value over a frame.

3.1 System equations for the non-work-conserving F-STE policy

Under this policy, packets can be served only after they have been shifted to the service queue, that is, only after the end of the frame over which they arrive. The server remains idle when the service queue is empty even if the data queues may be non-empty. This non-work-conserving version of the F-STE policy is considered primarily to facilitate the study of the F-STE policy presented afterwards. Nevertheless, this policy may be employed for applications in which the packets of the frame cannot be served before the packets of the entire frame have been received. It is easy to establish that the system process $\{Q_k, I_k\}_{k\geq 0}$ is a Markov chain, since I_k is a periodic Markov chain and Q_{k+1} is (probabilistically) determined from Q_k and A_m^k. The probability $P(i,j,i',j')$ that the Markov chain moves from state (i,j) to state (i',j') is given below. When $i \geq \tau$, the system queue cannot become empty between two successive shifts to the service queue, τ slots apart; when $i < \tau$, the service queue becomes empty between two successive shifts. Note that since only one packet can arrive over one slot, the maximum number of packets arriving over T time slots (one time frame) is T.

Case A : $\tau \leq i$

$$\begin{array}{lll} \text{For} & (i-\tau) \leq i' \leq T-1: & P(i,j,i',j') = P\{A_T^{j'} = i'-i+\tau\} \\ \text{For} & i' = T: & P(i,j,i',j') = \sum_{k=T-i+\tau}^{T} P\{A_T^{j'} = k\} \end{array} \tag{1}$$

Case B : $0 \leq i < \tau$

$$\text{For} \quad 0 \leq i' \leq T: \quad P(i,j,i',j') = P\{A_T^{j'} = i'\} \tag{2}$$

3.2 Auxiliary system equations for the work-conserving F-STE policy

According to the work-conserving F-STE policy, if the service queue becomes empty at some time t, $t_k < t < t_{k+1}$, the server attends to the data queues according to the ordered HoL priority $(I_{k+1}, \ldots, I_{k+N})$ (see section 2). An implication of this policy is that the system process $\{Q_k, I_k\}_{k\geq 0}$ is not a Markov chain. Some of the arrivals to be shifted into the data queue at t_{k+1}, given by $A_T^{I_{k+1}}$, may have already been served while in the corresponding data queue. Since the latter quantity is needed to determine the evolution of $\{Q_k, I_k\}_{k\geq 0}$, $\{Q_k, I_k\}_{k\geq 0}$ is not a Markov chain.

In order to obtain the system evolution for the work-conserving case, the Markovian process $\{Q_k, I_k, \bar{L_k}\}_{k\geq 0}$ can be considered, where $\bar{L_k}$ is an N-dimensional vector representing the occupancy of the data queues at time t_k. The resulting analysis would be involved and the complexity would be prohibitive for a large N. Nevertheless, this approach has been employed in the study of the work-conserving F-STE policy supporting $N = 2$ streams. The derivation of the system equations is not presented here due to space limitation. Only some results are presented at the end of the paper.

The work-conserving F-STE policy for large N is studied here by following the approach described below. This approach leads to the derivation of bounds and approximations on the performance of the work-conserving F-STE policy with a complexity similar to that for the non-work-conserving case, even for large N.

Since all packet losses (deadline violations) are "registered" as service queue overflows occurring at some t_k (when the corresponding data queue is shifted into the service queue), bounds on the packet loss under the work-conserving F-STE policy can be obtained by defining proper auxiliary systems U and L which are such that their service occupancies at times t_k – denoted by Q_k^u and Q_k^l respectively – satisfy

$$Q_k^l \leq Q_k \leq Q_k^u. \tag{3}$$

For properly selected auxiliary systems (policies), the above relationship would then lead to a similar one involving the corresponding packet loss probabilities given by

$$L_k^l \leq L_k \leq L_k^u. \tag{4}$$

Furthermore, by constructing the auxiliary system in a way that the system processes posses the Markovian property, the packet loss probabilities will be easily derived, as described in subsection 3.3.

Since the non-work-conserving F-STE scheduler remains idle when the service queue becomes empty, and is otherwise identical to the work-conserving F-STE scheduler, it is evident that the associated system can serve as the auxiliary system U. In 3.2.1, an auxiliary system L is proposed, and equations are derived for the system evolution. Another auxiliary system A is proposed in 3.2.2, in order to obtain a close approximation for the packet loss of the work-conserving F-STE policy. The following will be satisfied by this auxiliary system.

$$Q_k^l \leq Q_k^a \leq Q_k^u, \qquad L_k^l \leq L_k^a \leq L_k^u. \tag{5}$$

The tightness of the bounds and the accuracy of the approximate results are discussed in the last section where numerical results are presented.

3.2.1 Auxiliary system L

The auxiliary system L is defined to be similar to the system under the non-work-conserving F-STE policy with the following differences. If the service queue becomes empty before the next data queue shifting time t_{k+1}, the number of slots wasted under the non-work-conserving F-STE policy is considered as a service credit available at t_{k+1}; this amount is registered as an equivalent negative contribution to the service queue occupancy at t_{k+1}. There is an upper bound on the allowed credit accumulation equal to $T-\tau$. This bound is set by the requirement that earlier service credit cannot be utilized by future arrivals since it will be lost ("expired credit"). More specifically, service queue occupancy $x < \tau - T$ at t_k would imply the generation of at least $|x-(T-\tau)|$ credit units during the interval $(t_{k-N}, t_{k-(N-1)}]$; this credit must be wasted since all packets in the data queues at t_k have arrived after $t_{k-(N-1)}$.

The one-step transition probability for $\tau - T \leq i \leq T$ for system L is given by

$$\begin{array}{lll} \text{For} \quad i' = T: & P(i,j,i',j') = \sum_{k=T-i+\tau}^{T} P\{A_T^{j'} = k\} \\ \text{For} \quad (\tau - T) < i' < T-1: & P(i,j,i',j') = P\{A_T^{j'} = i' - i + \tau\} \\ \text{For} \quad i' = \tau - T: & P(i,j,i',j') = \sum_{k=0}^{2\tau - i - T} P\{A_T^{j'} = k\} \end{array} \tag{6}$$

3.2.2 Auxiliary system A

In deriving the evolution of system L, it was assumed that all the "unexpired" slots (inducing "unexpired" credit) wasted under the non-work-conserving policy could be utilized by serving the data queues. This is true only if at least one data queue is non-empty during the interval from when the service queue becomes empty, till the next shift to the service queue. In order to obtain a better approximation for the packet loss probability of the work-conserving F-STE policy, an auxiliary system A is considered, in which a more precise credit accumulation rule is applied. As in the case of the auxiliary system L, the service queue capacity i must satisfy $\tau - T \leq i \leq T$.

Case A : $i' > 0$

In this case, no service credit is generated.

$$\begin{array}{lll} \text{For} \quad (i-\tau) \leq i' \leq T-1: & P(i,j,i',j') = P\{A_T^{j'} = i' - i + \tau\} \\ \text{For} \quad i' = T: & P(i,j,i',j') = \sum_{k=T-i+\tau}^{T} P\{A_T^{j'} = k\} \end{array} \tag{7}$$

Case B : $i' \leq 0$

$[B1] : i > 0$

Unlike in system L, out of the $l = |i - \tau|$ non-used (by the packets in the service queue) service opportunities over $(t_k, t_{k+1}]$, only a portion will be registered as credit, based on the

number of (earlier) packet arrivals to the data queues which have not been shifted to the service queue at, or before, t_k. Thus, the actual amount of credits kept will be equal to $\min(|l|, \tilde{A_m})$ where $\tilde{A_m} = A^{j'+1}_{(N-2)\tau} + A^{j'+2}_{(N-3)\tau} + \ldots + A^{j'+N-2}_{\tau}$. Each of the terms in $\tilde{A_m}$ represents packet arrivals over some τ and for some stream which have not been shifted to the service queue at, or before, t_k. Arrivals over the interval $(t_k, t_{k+1}]$ over which this credit is generated are not considered since some of them may not arrive before the credit is generated; clearly, this is an approximation. In this case, the only possible transitions are to state i', where $-\tau < i' \leq 0$, and their probabilities are given by

$$P(i,j,i',j') = P\{A^{j'}_T = i' - i + \tau\} P\{\tilde{A_m} \geq |i'|\} + \sum_{k=0}^{i'-i+\tau-1} P\{A^{j'}_T = k\} P\{\tilde{A_m} = |i'|\} \qquad (8)$$

$[B2] : \tau - T \leq i \leq 0$

The service queue is empty at t_k, and $|i|$ service credits have already been accumulated. Let $l = i' - i$. If $l < 0$, $|l|$ is equal to the credit generated over $(t_k, t_{k+1}]$. Since packet arrivals to the data queues occuring before t_{k-1} have been considered toward the determination of the original credit $|i|$ (as indicated in the previous case, $[B1]$), only packet arrivals to the data queues occuring over $(t_{k-1}, t_k]$ will be used to determine the actual new credit to be kept. The latter arrivals are given by $\tilde{A_n} = A^{j'+1}_{\tau} + A^{j'+2}_{\tau} + \ldots + A^{j'+N-2}_{\tau}$. Finally, no credit is generated if $l \geq 0$. The transition probabilities are given by:

For $\tau - T < i' \leq 0$:

$$P(i,j,i',j') = \begin{cases} P\{A^{j'}_T = \tau + l\} & l > 0 \\ P\{A^{j'}_T = \tau + l\} P\{\tilde{A_n} \geq |l|\} + \sum_{k=0}^{\tau+l-1} P\{A^{j'}_T = k\} P\{\tilde{A_n} = |l|\} & l \leq 0 \end{cases} \qquad (9)$$

For $i' = \tau - T$:

$$P(i,j,i',j') = \begin{cases} P\{A^{j'}_T = \tau + l\} & l > 0 \\ \sum_{k=0}^{\tau+l} P\{A^{j'}_T = k\} P\{\tilde{A_n} \geq |l|\} & l \leq 0 \end{cases} \qquad (10)$$

3.3 Computation of packet loss probabilities

In view of the Markovian structure for the system processes defined in the previous subsections, the induced packet loss (deadline violation) probabilities are easy to determine. As indicated earlier, the packets whose deadline expires are precisely the packets which overflow from the service queue upon shifting to that queue.

Let L_{ij} denote the number of packets dropped over the interval $(t_k, t_{k+1}]$, where (i,j) is the system state at t_k. Notice that all losses will be associated with packets from stream $j' = (j+1) \bmod (N)$. Clearly,

$$L_{ij} = \left(A^{j'}_T + (i - \tau) - T\right)^+. \qquad (11)$$

Notice that at most $i - \tau$ packets may be lost since the maximum number of per stream and per frame arrivals is equal to T; no loss occurs if $i \leq \tau$. The average value of L_{ij}, $\bar{L_{ij}}$, is given by

$$\bar{L_{ij}} = \sum_{k=1}^{i-\tau} k P(A^{j'}_T = T - (i - \tau) + k). \qquad (12)$$

The loss rate for stream $j' = (j+1) \bmod (N)$ over $(t_k, t_{k+1}]$, when the system state at t_k is (i,j), is given by

$$R_{ij} = \frac{\bar{L_{ij}}}{\lambda^{j'} T}. \qquad (13)$$

Finally, the packet loss probability is given by

$$L = \sum_{i=\tau+1}^{T} \sum_{j=0}^{N-1} R_{ij} \pi(i,j), \qquad (14)$$

where $\pi(i,j)$ is the steady state distribution of the corresponding Markov chain.

4 Numerical Results

In this section, two sets of numerical results are presented. Figures 3 to 6 are derived to evaluate the accuracy of the bounds and approximations associated with the analysis of the general F-STE policy, as well as to present exact results for the non-work-conserving F-STE policy, and the work conserving F-STE policy with $N = 2$. Figures 7 and 8 are derived for the comparative evaluation of the F-STE and the FIFO policies.

The exact packet loss probability vs system utilization λ (for $T = 8$) for $N = 2$ streams served under the work-conserving F-STE are shown in Figure 3; simulations are also shown for verification of the equation (which are not presented in this paper). Results for systems U (non-work-conserving F-STE policy) and L are also shown.

Results for the packet loss probability for $N = 4$ streams vs system utilization λ (for $T = 8$) and vs frame length (for $\lambda = 0.88$) are presented in Figures 4 and 5, respectively. Results are shown for systems L, U, A, and simulations. For the cases considered here, the approximate system (system A) seems to provide for an accurate approximation of the performance of the work-conserving F-STE policy. The lower bound (auxiliary system L) is observed to be tighter than the upper bound (auxiliary system U, that is the non-work-conserving policy). As λ increases, the tightness of the lower bound improves since more of the unexpired credit in system L will actually be used under the work-conserving F-STE policy. Similarly, the tightness of the upper bound (non-work-conserving system) improves as λ increases since the server will be found idle less often and, thus, the work-conserving and non-work-conserving policies will tend to become identical. As T increases, the tightness of the upper bound deteriorates since the work-conserving and non-work-conserving F-STE policies become increasingly different and the server is found more frequently idle under system U while there is work in the system. The slight improvement of the tightness of the lower bound as T increases may be attributed to an increasing probability that a data queue is non empty and thus increasing amount of credit is kept. The impact of the number of streams N on the induced packet loss probability is illustrated in Figure 6 vs frame length T (for $\lambda = 0.88$); the results are for the work-conserving policy ($N = 2$, exact analysis) and for the approximate system A ($N = 4, 8, 16$).

Simulation results for the induced packet loss probability under the FIFO and work-conserving F-STE policies are shown in figures 7 and 8 vs system utilization λ (for $T = 16$ and $N = 4$) and vs frame length T (for $\lambda = 0.88$ and $N = 4$), respectively. The results from the analysis for the approximate system A are also shown. All results are derived for symmetric load.

As expected, the work-conserving F-STE policy always outperforms the FIFO policy. For high system utilization (Figure 7) the performance difference is small due to the scheduler throughput limitation. As λ decreases, the sub-optimality of the FIFO becomes a factor with increasing weight in inducing losses. As the frame length increases (Figure 8) the packet loss probability decreases under both policies. This may be attributed to the associated increase in the time to extinction as well as the increased smoothness of the cumulative traffic over a frame. The performance difference of the two policies is seen to increase as the frame length increases. This may again be attributed to increased sub-optimality of the FIFO policy: as the frame length increases, the range of extinction times of packets of the same frame increases leading to increased sub-optimality of the FIFO policy.

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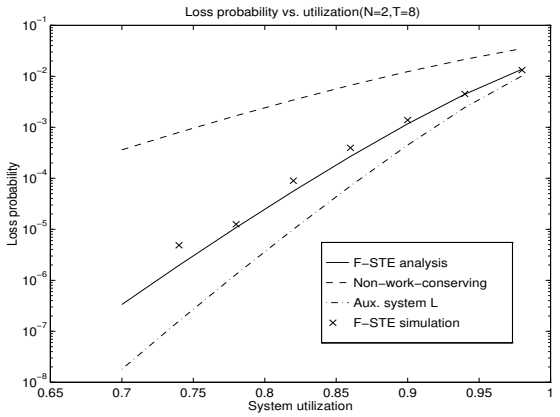

Figure 3: Analytical results for loss probability vs system utilization for $N = 2$ and $T = 8$.

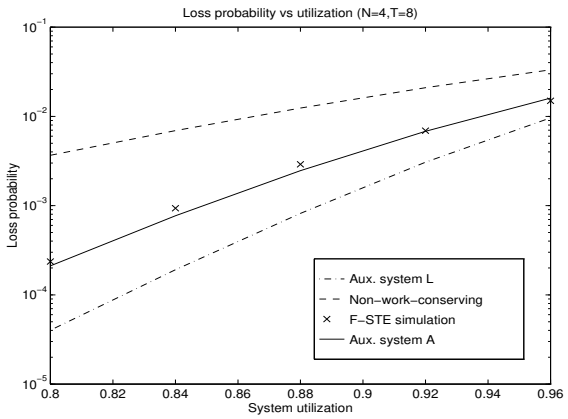

Figure 4: Analytical results for loss probability vs system utilization $N = 4$ and $T = 8$.

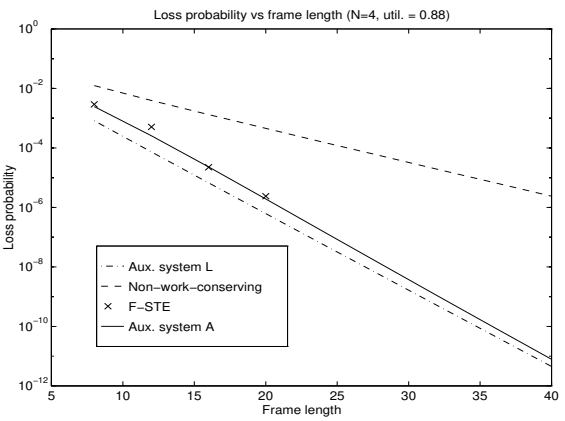

Figure 5: Analytical results for loss probability vs frame length $N = 4$ and system utilization equal to 0.88.

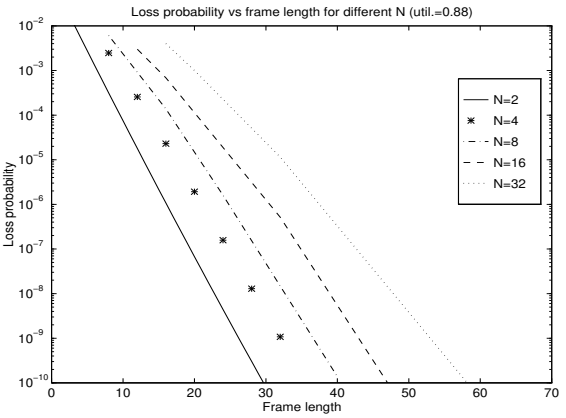

Figure 6: Analytical results for loss probability vs frame length, for different values of N given by system A for system utilization equal to 0.88.

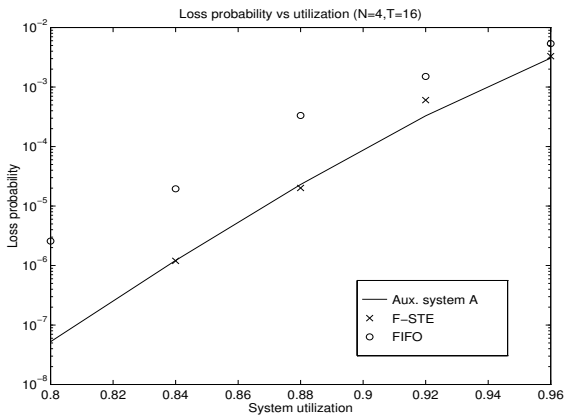

Figure 7: Loss probability vs system utilization for F-STE and FIFO for $N = 4$ and $T = 16$.

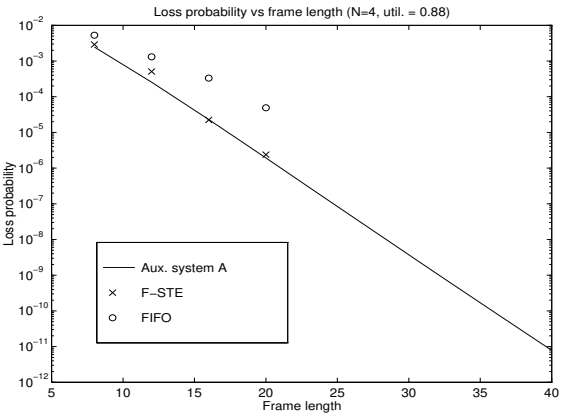

Figure 8: Loss probability versus frame length for F-STE and FIFO for $N = 4$ and system utilization equal to 0.88.