Cryptanalytic Attacks on Symmetric Ciphers or How to Design a Secure Cryptosystem

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Talk Outline

- Introduction Definitions
- O Mathematical analysis
 - Properties of cryptographic functions
- Security of modern ciphers
 - Security of cryptographic protocols
- Conclusions

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Symmetric ciphers Stream ciphers Block ciphers

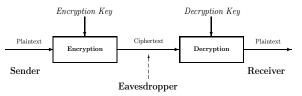
Cryptography in practice

- e-democracy: Need to build citizens' trust
 - Without trust, citizens will not visit portals, will not exchange data,...
- Security challenges: confidentiality (privacy), integrity, authentication, transparency
- Cryptographic primitives have a crucial role
 - Confidentiality of the transmitted data is mainly ensured by symmetric cryptography
 - Characteristic example: SSL/TLS protocol (underlying in the https connections)
 - Symmetric cryptography is also used in several other cases (wireless networks, mobile networks, RFID applications etc.)
- Aim of this talk: Overview of recent developments and current research trends

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Symmetric ciphers

A typical cryptosystem



Symmetric cryptography

- Encryption Key = Decryption Key
- The key is only shared between the two parties
 - The security rests with the secrecy of the key (Kerchoffs principle)

Two types of symmetric ciphers

- Stream ciphers
- Block ciphers

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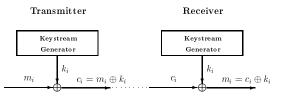
Attacks models

- Ciphertert-only attack
 - The attacker knows only the ciphertext
- Known-plaintext attack
 - The attacker also knows part of the plaintext
- Chosen-plaintext attack
 - It is assumed that the attacker is able to choose plaintexts to encrypt and, then, to observe the corresponding ciphertexts
- Chosen-ciphertext attack
 - It is assumed that the attacker is able to choose ciphertexts to decrypt and, then, to observe the corresponding plaintexts
- The last two types of attacks are more theoretical than practical.
 - However, a cipher is being considered as (computationally) secure only if all types of attacks require prohibitive computational cost

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Stream ciphers

Typical Case: Binary additive stream cipher



- Suitable in environments characterized by a limited computing power or memory, and the need to encrypt at high speed
- The seed of the keystream generators constitutes the secret key
- Security depends on
 - Pseudorandomness of the keystram k_i
 - Properties of the underlying functions that form the keystream generator

The optimal cipher: one-time pad

Description

- If $M = m_1 m_2 \dots m_n$, then $k = k_1 k_2 \dots k_n$ satisfying
 - \bullet k is trully random
 - \bullet k is aperiodic
 - For each different message, we use different key
- Encryption: $c_i = m_i \oplus k_i$, $i = 1, 2, \dots, n$
- Decryption: $m_i = c_i \oplus k_i$, $i = 1, 2, \dots, n$
- Such cipher is perfectly secure (Claude Shannon 1949)

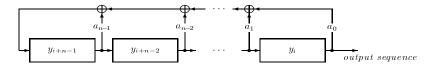
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$$p(M|C) = p(M)$$
 for any pair M, C

- However both randomness as well as aperiodicity can not be ensured in a realistic model
- Designing of stream ciphers strives to resemble the one-time pad

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Keystream Generators in stream ciphers

Basic building block: Linear Feedback Shift Register (LFSR)



Output sequence:

 $y_{i+n} = a_{n-1}y_{i+n-1} + \dots + a_1y_{i+1} + a_0y_i, \ a_j \in \{0,1\} \ \forall \ j = 0, 1, \dots, n-1$

- Easy implementation
- Nice mathematic properties
- But: The derived keystreams are easily predictable and, thus, cryptographically weak

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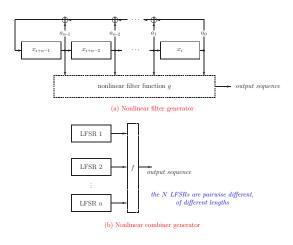
Predictability of keystreams: Linear complexity

- Linear complexity of a sequence: The length of the shortest LFSR that generates the sequence
- If the length of the keystream is N and its linear complexity is L, then the shortest LFSR is unique if and only if $L \leq \frac{N}{2}$
- Berlekamp-Massey algorithm: Efficient recursive computation of the shortest LFSR that generates a given sequence (Total complexity: $\mathcal{O}(N^2)$)
 - The same algorithm is also used for decoding famous error-control codes (BCH/Reed-Solomon codes)
- Knowledge of 2L consecutive bits of the keystream suffices to generate the remainder!!
 - $\bullet \Rightarrow \mathsf{High} \mathsf{ linear complexity is prerequisite in keystreams}$
 - Appropriate use of nonlinear functions

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Classical Keystream Generators



- High linear complexity is ensured by appropriately choosing the underlying Boolean functions
- If these functions though do not satisfy certain properties, the system may be vulnerable to attacks
- More recently, nonlinear FSRs are preferred (although their mathematics are not well-known)

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Known stream ciphers

• RC4

- $\bullet\,$ Used in WEP, WPA, SSL/TLS
- A5/1
 - Used in mobile telephony (GSM)
- E0
 - Used in Bluetooth protocol

eStream project (2004–2008): Effort to promote the design of efficient and compact stream ciphers suitable for widespread adoption.

- Finalists:
 - Software implementation: HC-128, Rabbit, Salsa20/12, SOSEMANUK
 - Hardware implementation: Grain v1, MICKEY 2.0, Trivium

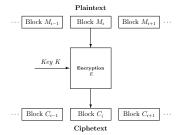
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Block ciphers

Typical Case: Electronic Codebook Mode (ECB)

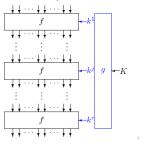


- Encryption on a per-block basis (typical block size: 128 bits)
- The encryption function E performs key-dependent substitutions and permutations (Shannon's principles)
- Security depends on
 - Generation of the sub-keys used in E
 - Properties of the underlying functions of E_{\downarrow}

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The encryption function E in a block cipher

- Iterative structure
 - Several rounds occur
- A sub-key is being used in each round
- The round function *f* performs substitution and permutations, via multi-output Boolean functions (S-boxes, P-boxes)
 - S-boxes and P-boxes provide the cryptographic properties of diffusion and confusion respectively (Claude Shannon 1949)

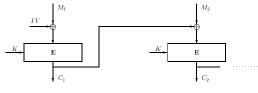


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Modes of operations for block ciphers

- In ECB mode, two identical message blocks are encrypted into identical ciphetext clocks
- Other modes of operation alleviate this issue: CBC, CFB, OFB, CTR modes
 - CBC may also used for constructing hash functions
 - CFB, OFB and CTR transform a block cipher into a (powerful) stream cipher

CipherBlock Chaining Mode of operation (CBC)



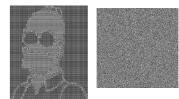
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ECB vs CBC

An example plaintext



Encrypted with AES in ECB and CBC mode



- Repeated patterns in a plainxtext is a realistic assumption, as shown in the example (obtained from a Bart Preneel's presentation, available online (MITACS, Toronto, 2010))
- Hence, ECB mode is of limited use

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Known block ciphers

• Advanced Encryption Standard (AES)

- NIST's standard since 2001 (initial submission: Rijndael cipher)
- Supported key lengths: 128, 192, 256 bits
- Widespread adoption (SSL/TLS, IPSec, commercial products,...)
- Data Encryption Standard (DES)
 - The predecessor of AES (1976-1996)
 - Official withdrawing: 2004 (although it is still being met today)
 - Key size: 56 bits (actually, the only flaw of the algorithm)
- 3DES
 - $\bullet\,$ Modification of DES, to use key of 112 or 168 bit length
 - Still in use today although not very efficient
- Other block ciphers: IDEA, MARS, RC6, Serpent, Twofish

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A common approach for block and stream ciphers

- Despite their differences, a common study is needed for their building blocks (multi-output and single-output Boolean functions respectively)
- The attacks in block ciphers are, in general, different from the attacks in stream ciphers and vice versa. However:
 - For both cases, almost the same cryptographic criteria of functions should be in place
- Challenges:
 - There are tradeoffs between several cryptographic criteria
 - The relationships between several criteria are still unknown
 - Constructing functions satisfying all the main criteria is still an open problem

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Boolean Functions

A Boolean function f on n variables is a mapping from \mathbb{F}_2^n onto \mathbb{F}_2

- The vector $f = (f(0, 0, \dots, 0), f(1, 0, \dots, 0), \dots, f(1, 1, \dots, 1))$ of length 2^n is the truth table of f
- The Hamming weight of f is denoted by wt(f)
 - f is balanced if and only if $wt(f) = 2^{n-1}$

• The support supp(f) of f is the set $\{b \in \mathbb{F}_2^n : f(b) = 1\}$ Example: Truth table of balanced f with n = 3

x_1	0	1	0	1	0	1	0	1
x_2	0	0	1	1	0	0	1	1
x_3	0	0	0	1 1 0	1	1	1	1
$f(x_1, x_2, x_3)$	0	1	0	0	0	1	1	1

A vectorial Boolean function f on n variables is a mapping from \mathbb{F}_2^n onto \mathbb{F}_2^m , m>1

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Algebraic Normal Form and degree of functions

• Algebraic Normal Form (ANF) of *f*:

$$f(x) = \sum_{\boldsymbol{v} \in \mathbb{F}_2^n} a_{\boldsymbol{v}} x^{\boldsymbol{v}}, \quad \text{where } x^{\boldsymbol{v}} = \prod_{i=1}^n x_i^{v_i}$$

• The sum is performed over \mathbb{F}_2 (XOR addition)

- The degree deg(f) of f is the highest number of variables that appear in a product term in its ANF.
- If $\deg(f) = 1$, then f is called affine function
 - If, in addition, the constant term is zero, then the function is called linear
- In the previous example: $f(x_1, x_2, x_3) = x_1x_2 + x_2x_3 + x_1$.

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$$\deg(f) = 2$$

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Univariate representation of Boolean functions

- \mathbb{F}_2^n is isomorphic to the finite field \mathbb{F}_{2^n} ,
- ⇒ Any function f ∈ B_n can also be represented by a univariate polynomial, mapping F_{2ⁿ} onto F₂, as follows

$$f(x) = \sum_{i=0}^{2^n - 1} \beta_i x^i$$

where $\beta_0, \beta_{2^n-1} \in \mathbb{F}_2$ and $\beta_{2i} = \beta_i^2 \in \mathbb{F}_{2^n}$ for $1 \le i \le 2^n - 2$

- The coefficients of the polynomial determine the Discrete Fourier Transform of f
- The univariate representation is more convenient in several cases

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Correlation immunity

- If the output of a Boolean function *f* is correlated to at least one of its inputs, then it is vulnerable to correlation attacks.
- The $f \in \mathbb{B}_n$ is *t*-th correlation immune if it is not correlated with any *t*-subset of $\{x_1, \ldots, x_n\}$; namely if

$$Pr(f(\boldsymbol{x}) = 0 | x_{i_1} = b_{i_1}, \dots, x_{i_t} = b_{i_t}) = Pr(f(\boldsymbol{x}) = 0)$$

for any t positions x_{i_1},\ldots,x_{i_t} and any $b_{i_1},\ldots,b_{i_t}\in\mathbb{F}_2$

- If a *t*-th order correlation immune function is also balanced, then it is called *t*-th order resilient.
- A known trade-off: If f is k-th order resilient for $1 \le k \le n-2$, then $\deg(f) \le n-k-1$.

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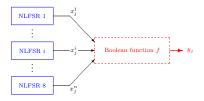
Linear approximation attacks

- Cryptographic functions need to be balanced, as well as of high degree
 - $\bullet\,$ The maximum possible degree of a balanced Boolean function with n variables is n-1
- High degree though is not adequate to prevent linear cryptanalysis (in block ciphers - Matsui, 1992) or best affine approximation attacks (in stream ciphers - Ding et. al., 1991)
 - A function should not be well approximated by a linear/affine function
 - Any function of degree 1 that best approximates f is a best affine/linear approximation of f

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Example of approximation attacks

The Achterbahn cipher [Gammel-Göttfert-Kniffler,2005] (candidate in eSTREAM project)



- Lengths of nonlinear FSRs: 22-31
- $f(x_1, \ldots, x_8) = \sum_{i=1}^4 x_i + x_5 x_7 + x_6 x_7 + x_6 x_8 + x_5 x_6 x_7 + x_6 x_7 x_8$
- Johansson-Meier-Muller, 2006: cryptanalysis via the linear approximation $g(x_1, \ldots, x_8) = x_1 + x_2 + x_3 + x_4 + x_6$, satisfying wt(f + g) = 64 (p(f = g) = 3/4)

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The notion of nonlinearity

• The minimum distance between *f* and all affine functions is the nonlinearity of *f*:

$$\mathsf{nl}(f) = \min_{l \in \mathbb{B}_n : \deg(l) = 1} \operatorname{wt}(f+l)$$

- Nonlinearity is computed via the Fast Walsh Transform
- High nonlinearity is prerequisite for thwarting attacks based on affine (linear) approximations
- Constructions of correlation-immune functions with high nonlinearity exist (Maiorana-McFarland class (Camion-Carlet-Charpin-Sendrier, 1992),...)

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Known results on nonlinearity of Boolean functions

- For even n, the maximum possible nonlinearity is $2^{n-1} 2^{n/2-1}$, achieved by the so-called bent functions
 - Several constructions of bent functions are known
 - But bent functions are never balanced!
- For odd n, the maximum possible nonlinearity is still unknown
 - By concatenating bent functions, we can get nonlinearity $2^{n-1} 2^{\frac{n-1}{2}}$. Can we impove this?
 - For $n \leq 7$, the answer is no
 - For $n \ge 15$, the answer is yes (Patterson-Wiedemann, 1983 Dobbertin, 1995 Maitra-Sarkar, 2002)
 - For n = 9, 11, 13, such functions have been found more recently (Kavut, 2006)
- Several constructions of balanced functions with high nonlinearity exist. However:
 - Finding the highest possible nonlinearity of balanced Boolean functions is still an open problem

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Higher-order nonlinearity

- Approximating a function by a low-order function (not necessarily linear) may also lead to cryptanalysis (Non–linear cryptanalysis -Knudsen-1996, low-order approximation attacks - Kurosawa et. al. -2002)
- The rth order nonlinearity of a Boolean function $f \in \mathbb{B}_n$ is given by

$$\mathsf{nl}_r(f) = \min_{g \in \mathbb{B}_n : \deg(g) \le r} \operatorname{wt}(f+g)$$

- The rth order nonlinearity remains unknown for r > 1
 - Recursive lower bounds on $nl_r(f)$ (Carlet, 2008)
 - Specific lower and upper bounds for nl₂(*f*) (Cohen, 1992 Carlet, 2007)
 - More recent lower bounds for 2-nd order nonlinearity: Gangopadhyay et. al. 2010, Garg et. al. 2011, Singh 2011, Singh et. al. 2013

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Computing best low order approximations

- Computing even the best 2-nd order approximations is a difficult task
 - Efficient solution for specific class of 3-rd degree functions (Kolokotonis-Limniotis-Kalouptsidis, 2009)
 - The problem is appropriately reduced in computing best affine approximation attacks of the underlying 2-nd degree sub-functions
 - For the Achterbahn's combiner function:

 $q(x) = x_5x_7 + x_6x_8 + x_1 + x_2 + x_3 + x_4$ is a best 2-nd approximation

•
$$wt(f+q) = 32 (p(f=q) = 7/8 > 3/4)$$

- No much is known regarding constructions of functions with high r-th nonlinearity, for $r\geq 2$
 - A class of highly nonlinear 3-rd degree functions satisfying $nl_2(f) = nl(f)$ (Kolokotronis-Limniotis, 2012)

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More recent attacks: Algebraic attacks

Milestones

- Algebraic attacks (Courtois-Meier, 2003)
- Fast algebraic attacks (Courtois, 2003)
- The basic idea is to reduce the degree of the mathematical equations employing the secret key
- Known cryptographic Boolean functions failed to thwart these attacks
- Some applications of algebraic attacks
 - Six rounds of DES, with only one known plaintext (Courtois-Bard, 2006)
 - Keeloq block cipher (Courtois-Bard-Wagner, 2008)
 - Hitag2 stream cipher (Courtois et. al., 2009)

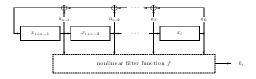
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Algebraic attacks

Example

• Stream cipher based on a nonlinear filter generator



- $k_i = f(L^i(x_0, x_1, \dots, x_{N-1}))$ the filter function f has high degree
- Assume that there exists $g \in \mathbb{B}_n$ of low degree such that f * g = h, where h is also of low degree. Then,

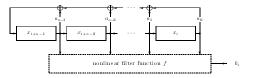
$$k_i g(L^i(x_0, x_1, \dots, x_{N-1})) = h(L^i(x_0, x_1, \dots, x_{N-1}))$$

• Several other proper choices of g, h may also reduce the degree of the system

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An example: The Toyocrypt cipher

• A submission to a Japanese government call



• The nonlinear filter function is

$$f(x_1, \dots, x_{128}) = q(x_1, \dots, x_{128}) + x_{10}x_{23}x_{32}x_{42} + \prod_{i=1}^{62} x_i +$$

 $+ x_1 x_2 x_9 x_{12} x_{18} x_{20} x_{23} x_{25} x_{26} x_{28} x_{33} x_{38} x_{41} x_{42} x_{51} x_{53} x_{59}$

where $\deg(q) = 2$.

• By multiplying f with the affine functions $1 + x_{23}$ or $1 + x_{42}$, we get two functions of degree only 3

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How to proceed with algebraic attacks

- Once the degree of the equations have been reduced, several algebraic techniques have been proposed for solving the (still nonlinear) system:
 - Linearization of the system
 - Use of Gröbner bases
 - More specific techniques: XL, XSL
- Hence, the core of the algebraic attacks is the transformation of the initial system to a new one having low degree

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Annihilators and algebraic immunity

Definition

Given $f \in \mathbb{B}_n$, we say that $g \in \mathbb{B}_n$ is an annihilator of f if and only if g lies in the set

$$\mathcal{AN}(f) = \{g \in \mathbb{B}_n : f * g = 0\}$$

Definition

The algebraic immunity $AI_n(f)$ of $f \in \mathbb{B}_n$ is defined by

$$\mathsf{Al}_n(f) = \min_{g \neq 0} \{ \deg(g) : g \in \mathcal{AN}(f) \cup \mathcal{AN}(f+1) \}$$

- A high algebraic immunity is prerequisite for preventing algebraic attacks (Meier-Pasalic-Carlet, 2004)
- Well-known upper bound: $AI_n(f) \leq \lceil \frac{n}{2} \rceil$

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Some properties of algebraic immunity

Low nonlinearity implies low algebraic immunity: (Carlet et. al., 2006)

$$\mathsf{nl}_r(f) \ge \sum_{i=0}^{\mathsf{Al}_n(f)-r-1} \binom{n}{i}$$

Especially for r = 1: (Lobanov, 2005)

$$\mathsf{nl}(f) \geq 2\sum_{i=0}^{\mathsf{Al}_n(f)-2} \binom{n-1}{i}$$

Rizomiliotis, 2010: Improvements on the above bounds

• The notion of partial algebraic immunity is defined

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Fast algebraic attacks

- Consider again the filter generator: $k_i = f(L^i(x_0, x_1, \dots, x_{N-1}))$
- Assume that there exists a low degree $g \in \mathbb{B}_n$ such that h = f * g is of reasonable degree. Then again,

$$k_i g(L^i(x_0, x_1, \dots, x_{N-1})) = h(L^i(x_0, x_1, \dots, x_{N-1}))$$

• There exists a linear combination of the first $\sum_{i=0}^{\deg(h)} {N \choose i}$ equations that sum the right-hand part to zero \Rightarrow We get one equation of degree at most $\deg(g)$

Comparison with conventional algebraic attacks

- $g + h \in \mathcal{AN}(f) \Rightarrow$ the degree of g + h may be greater than $\mathsf{AI}_n(f)$,
 - Maximum AI does not imply resistance to fast algebraic attacks
- But: Knowledge of consecutive keystream bits is required

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Fast Algebraic Immunity

Known result: For any pair of integers (e, d) such that $e + d \ge n$, there exists a nonzero function g of degree at most e such that f * g has degree at most d.

Definition

The fast algebraic immunity $FAI_n(f)$ of $f \in \mathbb{B}_n$ is defined by

$$\mathsf{FAI}_n(f) = \min_{1 \leq \deg(g) \leq \mathsf{AI}_n(f)} \{ 2 \, \mathsf{AI}_n(f), \deg(g) + \deg(f \ast g) \}$$

• Upper bound: $FAI_n(f) \le n$

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Constructions of functions with maximum AI

- Dalai-Maitra-Sarkar, 2006: Majority function
 - For even *n*, a slight modification of the majority function also preserves maximum AI
- Carlet-Dalai-Gupta-Maitra-Sarkar, 2006: Iterative construction
- Li-Qi, 2006: Modification of the majority function
- Sarkar-Maitra, 2007: Rotation Symmetric functions of odd n
- Carlet, 2008: Based on properties of affine subspaces
 - Further investigation in Carlet-Zeng-Li-Hu, 2009
 - Generalization (for odd *n*) in Limniotis-Kolokotronis-Kalouptsidis, 2011
- Balanceness and/or high nonlinearity are not always attainable, whereas their fast algebraic immunity remains unknown

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Constructions of functions with maximum AI (Cont.)

- Carlet-Feng, 2008: $\operatorname{supp}(f) = \{0, 1, \alpha, \alpha^2, \dots, \alpha^{2^{n-1}-2}\}$, where α a primitive element of the finite field \mathbb{F}_{2^n} .
 - Balanceness and high (first-order) nonlinearity are ensured
 - Optimal against fast algebraic attacks, as subsequently shown (Liu-Zhang-Lin, 2012)

• Generalizations: Rizomiliotis (2010), Zeng-Carlet-Shan-Hu (2011)

• Proper modifications of the Carlet-Feng construction (via the univariate representation of the function)

• Further generalizations in Limniotis-Kolokotronis-Kalouptsidis (2013)

- $\bullet~{\rm Finding~swaps}$ between ${\rm supp}(f)$ and ${\rm supp}(f+1)$ that preserve maximum AI
- Still room for research regarding fast algebraic immunity (and r-th order nonlinearity for $r \ge 2$)

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Current status

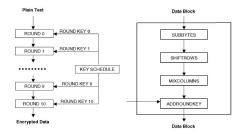
Open problems in the area

- Relationships between (fast) algebraic immunity and correlation immunity
 - The trade-off between correlation immunity and degree directly implies a trade-off between correlation immunity and fast algebraic immunity
- Evaluation of known families of cryptographic functions in terms of resistance against (fast) algebraic attacks
- Construction of functions with maximum (fast) algebraic immunity
 - Much progress on constructing functions with maximum AI, but the case of maximum FAI is much more difficult
- Nonlinear FSRs (or other nonlinear structures) have not been studied to the same extent

AES RC4 Ciphers in security protocols

Design principles of AES

AES operation (key size=128 bits) - (Daemen-Rijmen, 1997)



- The S-box (SubByte) is a highly nonlinear function
- Designed to be resistant against all known cryptanalytic attacks
- The inherent algebraic structures (Murphy-Robshaw, 2002) do not allow mounting algebraic attacks

AES RC4 Ciphers in security protocols

Recent attacks on AES

- The most important: A related-key attack for key lengths 192 and 256 bits (Biryukov et. al. 2009)
 - Practical attacks for reduced number of rounds
 - Although such attacks are generally more theoretical than practical
 - It raises concern about the security margin of the AES
 - B. Schneier (2009): "(...) for new applications I suggest that people don't use AES-256. AES-128 provides more than enough security margin for the foreseeable future. But if you're already using AES-256, there's no reason to change".

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AES RC4 Ciphers in security protocols

Side-channel cryptanalysis

Timing attacks in AES

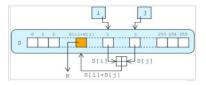
- Cryptanalysis using additional information from the implementation of the algorithm
- The MixColumns function of AES may have different execution times, depending on the corresponding values
- Measuring the execution time provides information for the secret key
 - Most powerful timing attack on AES: Bernstein, 2005
- Conclusion: Not only mathematics, but implementation issues also need to be considered

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AES **RC4** Ciphers in security protocols

Weaknesses depending on algorithm's parameters

The RC4 cipher (Rivest, 1987)



- i, j are updated via a specific procedure
- The weaknesses mainly stem from the keystream generator
 - The first bytes of K do not possess pseudorandom characteristics
- Proper choice of parameters is needed (key size, discarding first bytes of keystream,...)
- Academically not secure (distinguishing attacks)
 - Still secure though in practice (under a proper choice of parameters)
 - But....

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Secure cipher does not imply secure protocol

RC4 in encryption protocols

- WEP is not considered as secure (see e.g. Tews et. al. 2007: Breaking 104 bit WEP in less than 60 seconds)
 - Flaws rest with implementation (e.g. not proper choices of Initilization Vectors)
- AlFardan, Bernstein, Paterson, Poettering, Schuldt 2013: Security of RC4 encryption in TLS and WPA/TKIP has been compromised
- From www.isg.rhul.ac.uk/tls:
 - The attacks in TLS arise from statistical flaws in the keystream generated
 - Most effective countermeasure: Stop using RC4 in TLS
 - $\bullet\,$ One of the attacks also applies to WPA/TKIP
 - Most effective countermeasure: Upgrade to WPA2

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Even AES may not provide a secure protocol

Attacks in IPSec

- IPSec provides security at the IP Layer (mainly used in Virtual Private Networks)
- Paterson-Yau, 2006 Degabriel-Paterson, 2007: Active ciphertext-only attacks, if only encryption (and not data authentication) is implemented
 - Encryption with AES
 - Even following RFCs may not be enough!
- The attacks rest with the CBC mode of AES
 - Flipping bits in a ciphertext block leads to controlled changes in the subsequent decrypted plaintext block
 - Example: Appropriate modification of headers so that error messages, carrying plaintext data, are sent to attacker's machine

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Conclusions

- Mathematics for ensuring cryptographic properties that are prerequisite to withstand any type of known attacks
 - Always leave a security margin the attacks are getting better and better
- A secure cipher does not imply secure protocol
 - A proper design of the protocol is needed
- B. Schneier, Sep. 2013 (after disclosures of NSA eavesdropping on the Internet):
 - "(...) Remember this: The math is good, but math has no agency. Code has agency, and the code has been subverted (...)"
 - "(...) Trust the math. Encryption is your friend. Use it well, and do your best to ensure that nothing can compromise it (...)"

Questions & Answers

Thank you for your attention!

K. Limniotis Cryptanalytic attacks on symmetric ciphers

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