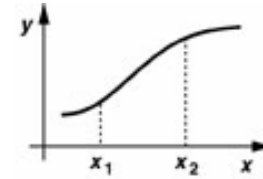


ΕΝΙΣΧΥΤΕΣ ΜΙΑΣ ΒΑΘΜΙΔΑΣ

Βασικές Έννοιες

$$y(t) \approx \alpha_0 + \alpha_1 x(t) + \alpha_2 x^2(t) + \dots + \alpha_n x^n(t) \quad x_1 \leq x \leq x_2$$

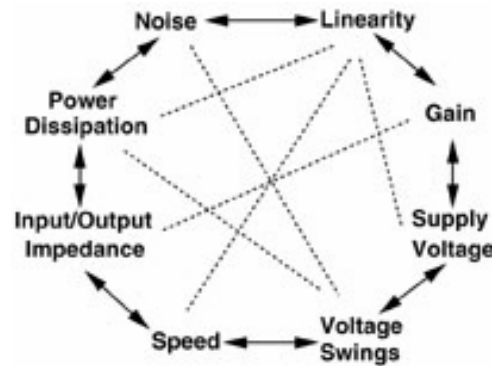


$$y(t) \approx \alpha_0 + \alpha_1 x(t)$$

$$\alpha_1 x(t) \ll \alpha_0$$

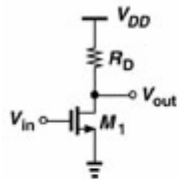
$$\Delta y = \alpha_1 \Delta x$$

Το οκτάγωνο της αναλογικής σχεδίασης

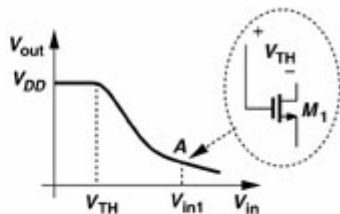


Βαθμίδα κοινής πηγής

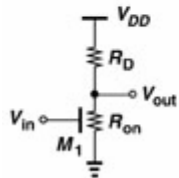
Βαθμίδα κοινής πηγής με φόρτο ωμική αντίσταση



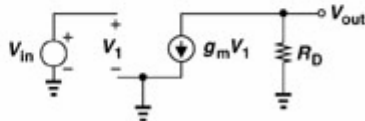
(a)



(b)



(c)



(d)

Για $V_{in}=0 \Rightarrow V_{out}=V_{DD}$

Για $V_{in} > V_{TH}$, $V_{out} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2$

Για $V_{out} = V_{in1} - V_{TH}$, $V_{in1} - V_{TH} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{TH})^2$,

Για $V_{in} > V_{in1}$, $V_{out} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} [2(V_{in} - V_{TH})V_{out} - V_{out}^2]$.

Για $V_{in} \gg V_{TH}$, $V_{out} \ll 2(V_{in} - V_{TH})$,

$$V_{out} = V_{DD} \frac{R_{on}}{R_{on} + R_D} = \frac{V_{DD}}{1 + \mu_n C_{ox} R_D \frac{W}{L} (V_{in} - V_{TH})}$$

$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = -R_D \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH}) = -g_m R_D$$

$$A_v = -\sqrt{2\mu_n C_{ox} \frac{W}{L} I_D} \frac{V_{RD}}{I_D} = -\sqrt{2\mu_n C_{ox} \frac{W}{L} \frac{V_{RD}}{I_D}}$$

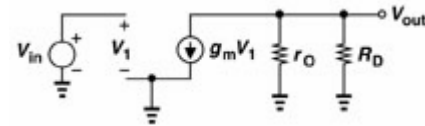
Για $R_D \gg r_D$

$$V_{out} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2 (1 + \lambda V_{out}),$$

$$\frac{\partial V_{out}}{\partial V_{in}} = -R_D \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH}) (1 + \lambda V_{out}) - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2 \lambda \frac{\partial V_{out}}{\partial V_{in}}$$

$$A_v = -R_D g_m - R_D I_D \lambda A_v \Rightarrow A_v = -\frac{g_m R_D}{1 + R_D \lambda I_D}$$

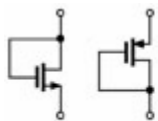
$$A_v = -g_m \frac{r_D R_D}{r_D + R_D}$$



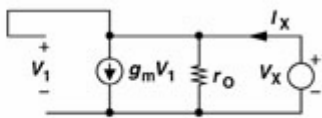
Ενδογενής απολαβή

$$A_{vmax} = -g_m r_D$$

Βαθμίδα κοινής πηγής με φόρτο MOSFET σε συνδεσμολογία διόδου

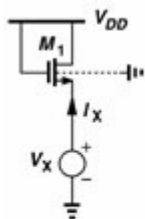


(a)

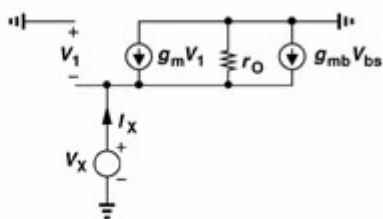


(b)

$$\frac{V_x}{I_x} = \frac{1}{g_m} // r_D \approx \frac{1}{g_m}$$



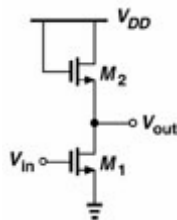
(a)



(b)

$$(g_m + g_{mb})V_x + \frac{V_x}{r_D} = I_x$$

$$\frac{V_x}{I_x} = \frac{1}{g_m + g_{mb} + r_D^{-1}} = \frac{1}{g_m + g_{mb}} // r_D \approx \frac{1}{g_m + g_{mb}}$$



$$A_v = -g_{m1} \frac{1}{g_{m2} + g_{mb2}} = -\frac{g_{m1}}{g_{m2}} \frac{1}{1 + \eta}$$

$$\eta = \frac{g_{mb}}{g_m}$$

$$A_v = -\frac{\sqrt{2\mu_n C_{ox}} (W/L)_1 I_{D1}}{\sqrt{2\mu_n C_{ox}} (W/L)_2 I_{D2}} \frac{1}{1 + \eta} = -\frac{\sqrt{(W/L)_1}}{\sqrt{(W/L)_2}} \frac{1}{1 + \eta}$$

Γραμμική απόκριση όσο το M1 είναι στον κόρο.

Ανάλυση μεγάλου σήματος

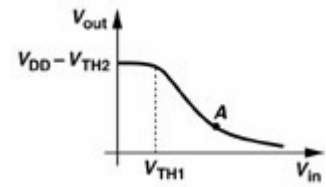
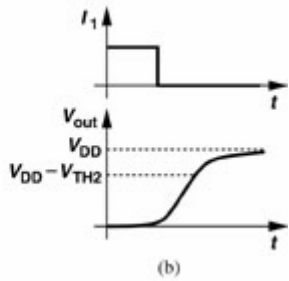
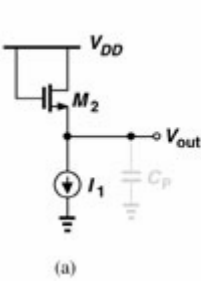
$$\frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_1 (V_{in} - V_{TH1})^2 = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 (V_{DD} - V_{out} - V_{TH2})^2,$$

$$\sqrt{\left(\frac{W}{L}\right)_1} (V_{in} - V_{TH1}) = \sqrt{\left(\frac{W}{L}\right)_2} (V_{DD} - V_{out} - V_{TH2}).$$

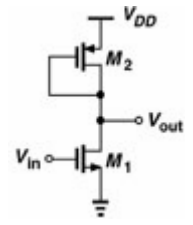
$$\sqrt{\left(\frac{W}{L}\right)_1} = \sqrt{\left(\frac{W}{L}\right)_2} \left(-\frac{\partial V_{out}}{\partial V_{in}} - \frac{\partial V_{TH2}}{\partial V_{in}}\right),$$

όπου $\frac{\partial V_{TH2}}{\partial V_{in}} = \frac{\partial V_{TH2}}{\partial V_{out}} \cdot \frac{\partial V_{out}}{\partial V_{in}} = \eta \cdot \frac{\partial V_{out}}{\partial V_{in}} \Rightarrow$

$$\frac{\partial V_{out}}{\partial V_{in}} = -\frac{\sqrt{(W/L)_1}}{\sqrt{(W/L)_2}} \frac{1}{1 + \eta}$$



PMOS



$$A_v = -\frac{\sqrt{\mu_n(W/L)_1}}{\sqrt{\mu_p(W/L)_2}}$$

Απαλλαγμένο από το φαινόμενο σώματος

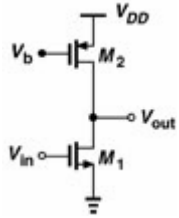
$$\mu_n \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{TH1})^2 \approx \mu_p \left(\frac{W}{L}\right)_2 (V_{GS2} - V_{TH2})^2,$$

$$\frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}} \approx A_v.$$

Με τη διαμόρφωση μήκους καναλιού

$$A_v = -g_{m1} \left(\frac{1}{g_{m2}} // r_{D1} // r_{D2} \right),$$

Βαθμίδα κοινής πηγής με φόρτο πηγής ρεύματος



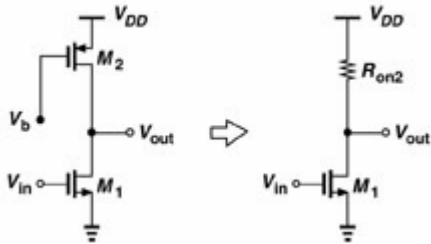
$$A_v = -g_{m1}(r_{D1} // r_{D2}).$$

Ενδογενής απολαβή

$$g_{m1}r_{D1} = \sqrt{2\left(\frac{W}{L}\right)_1 \mu_n C_{ox} I_D} \frac{1}{\lambda I_D}$$

Η γραμμική περιοχή μπορεί να αυξηθεί με αύξηση του $(W/L)_2$

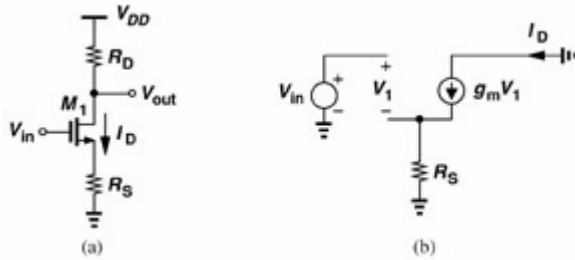
Βαθμίδα κοινής πηγής με φόρτο στην περιοχή τριόδου



$$R_{on2} = \frac{1}{\mu_p C_{ox} \left(\frac{W}{L}\right)_2 (V_{DD} - V_b - |V_{THP}|)}$$

Μειονέκτημα: εξάρτηση από τις παραμέτρους.

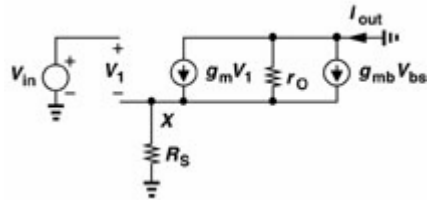
Βαθμίδα κοινής πηγής με ανασύζευξη (εκφυλισμό) πηγής



$$I_D = f(V_{GS})$$

$$G_m = \partial I_D / \partial V_{in} = \frac{\partial f}{\partial V_{GS}} \frac{\partial V_{GS}}{\partial V_{in}} = (1 - R_S \frac{\partial I_D}{\partial V_{in}}) \frac{\partial f}{\partial V_{GS}} \Rightarrow G_m = \frac{g_m}{1 + g_m R_S}$$

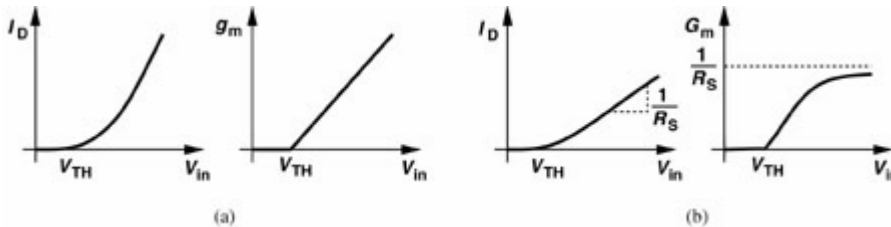
$$A_v = -G_m R_D = \frac{-g_m R_D}{1 + g_m R_S}$$



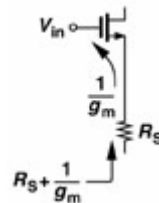
Υπολογισμός της διαγωγιμότητας αν συμπεριλάβουμε το φαινόμενο σώματος και τη διαμόρφωση μήκους καναλιού:

$$I_{out} = g_m V_1 - g_{mb} V_X - \frac{I_{out} R_S}{r_D} = g_m (V_{in} - I_{out} R_S) + g_{mb} (-I_{out} R_S) - \frac{I_{out} R_S}{r_D}$$

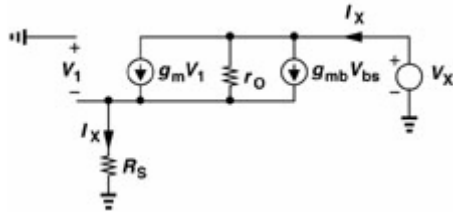
$$G_m = \frac{I_{out}}{V_{in}} = \frac{g_m r_D}{R_S + [1 + (g_m + g_{mb}) R_S] r_D}$$



$$A_v = -\frac{R_D}{(1/g_m) + R_S}$$



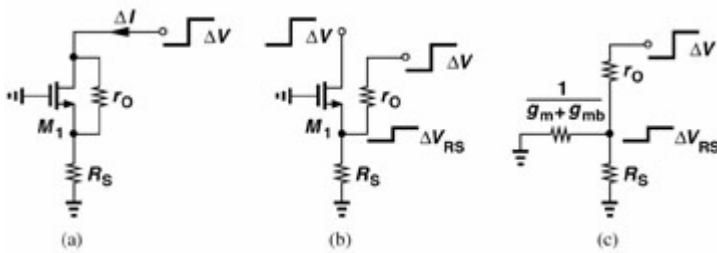
Υπολογισμός της αντίστασης εξόδου



$$r_D [I_X + (g_m + g_{mb}) R_S I_X] + I_X R_S = V_X$$

$$R_{out} = [1 + (g_m + g_{mb}) R_S] r_D + R_S = [1 + (g_m + g_{mb}) r_D] R_S + r_D$$

$$R_{out} \approx (g_m + g_{mb}) r_D R_S + r_D = [1 + (g_m + g_{mb}) R_S] r_D \Rightarrow R_{out} \gg r_D$$



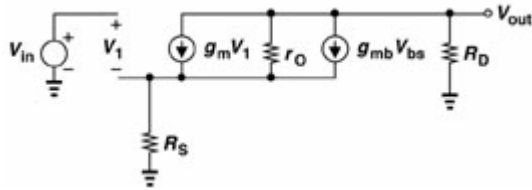
$$\Delta V_{RS} = \Delta V \frac{\frac{1}{g_m + g_{mb}} // R_S}{\frac{1}{g_m + g_{mb}} // R_S + r_D}$$

$$\Delta I = \frac{\Delta V_{RS}}{R_S} = \Delta V \frac{1}{[1 + (g_m + g_{mb}) R_S] r_D + R_S}$$

$$\frac{\Delta V}{\Delta I} = [1 + (g_m + g_{mb}) R_S] r_D + R_S$$

Υπολογισμός της απολαβής

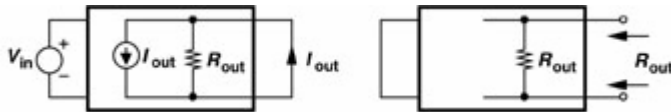
$$I_{r0} = -\frac{V_{out}}{R_D} - (g_m V_1 + g_{mb} V_{bs}) = -\frac{V_{out}}{R_D} - \left[g_m \left(V_{in} + V_{out} \frac{R_S}{R_D} \right) + g_{mb} V_{out} \frac{R_S}{R_D} \right]$$



$$V_{out} = I_{r0} R_D - \frac{V_{out}}{R_D} R_S = -\frac{V_{out}}{R_D} R_D - \left[g_m \left(V_{in} + V_{out} \frac{R_S}{R_D} \right) + g_{mb} V_{out} \frac{R_S}{R_D} \right] R_D - V_{out} \frac{R_S}{R_D}$$

$$\frac{V_{out}}{V_{in}} = \frac{-g_m r_D R_D}{R_D + R_S + r_D + (g_m + g_{mb}) R_S r_D}$$

$$A_v = \frac{-g_m r_D R_D [R_S + r_D + (g_m + g_{mb}) R_S r_D]}{R_D + R_S + r_D + (g_m + g_{mb}) R_S r_D} \cdot \frac{1}{R_S + r_D + (g_m + g_{mb}) R_S r_D} = -\frac{g_m r_D}{R_S + r_D + (g_m + g_{mb}) R_S r_D} \cdot \frac{R_D [R_S + r_D + (g_m + g_{mb}) R_S r_D]}{R_D + R_S + r_D + (g_m + g_{mb}) R_S r_D}$$



$$V_{out} = -I_{out} R_{out}, G_m = I_{out} / V_{in} \Rightarrow V_{out} = -G_m V_{in} R_{out} \Rightarrow A_v = -G_m R_{out}$$