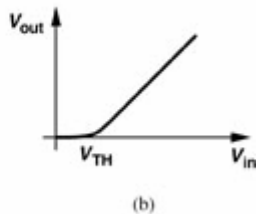
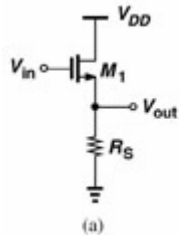


Ακολουθητής πηγής



$$A_v \quad V_{in} < V_{TH} \Rightarrow V_{out} = 0$$

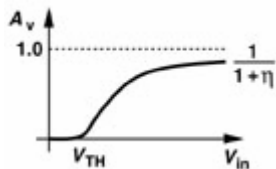
$$A_v \quad V_{in} > V_{TH} \Rightarrow \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH} - V_{out})^2 R_S = V_{out}$$

$$\text{Επειδή για } V_{in} \leq V_{DD} \quad \text{πάντοτε} \quad V_{DS} > V_{GS} - V_T$$

$$\frac{1}{2} \mu_n C_{ox} \frac{W}{L} 2(V_{in} - V_{TH} - V_{out}) \left(1 - \frac{\partial V_{TH}}{\partial V_{in}} - \frac{\partial V_{out}}{\partial V_{in}}\right) R_S = \frac{\partial V_{out}}{\partial V_{in}}$$

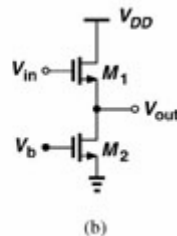
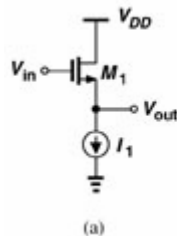
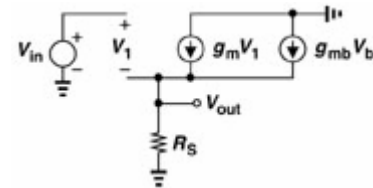
$$\frac{\partial V_{TH}}{\partial V_{in}} = \eta \frac{\partial V_{out}}{\partial V_{in}}$$

$$\frac{\partial V_{out}}{\partial V_{in}} = \frac{\mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH} - V_{out}) R_S}{1 + \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH} - V_{out}) R_S (1 + \eta)}$$

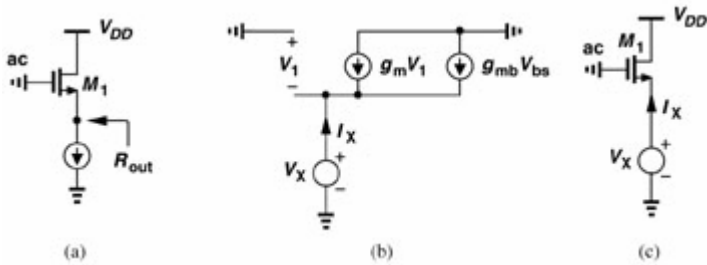


$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH} - V_{out})$$

$$A_v = \frac{g_m R_S}{1 + (g_m + g_{mb}) R_S}$$

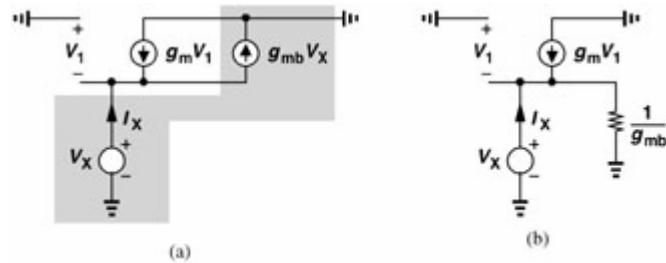


Αντίσταση εξόδου

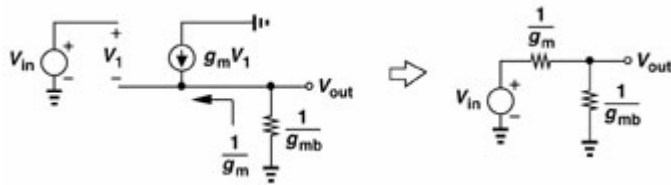


$$I_x - g_m V_x - g_{mb} V_x = 0$$

$$R_{out} = \frac{1}{g_m + g_{mb}}$$

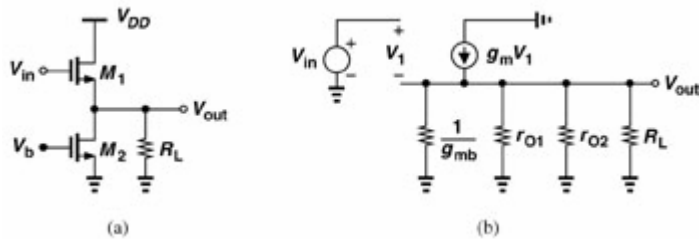


$$R_{out} = \frac{1}{g_m} \parallel \frac{1}{g_{mb}} = \frac{1}{g_m + g_{mb}}$$



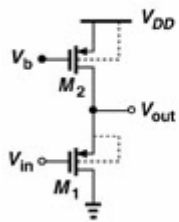
$$A_v \ R_S = \infty \Rightarrow$$

$$A_v = \frac{\frac{1}{g_{mb}}}{\frac{1}{g_m} + \frac{1}{g_{mb}}} = \frac{g_m}{g_m + g_{mb}}$$

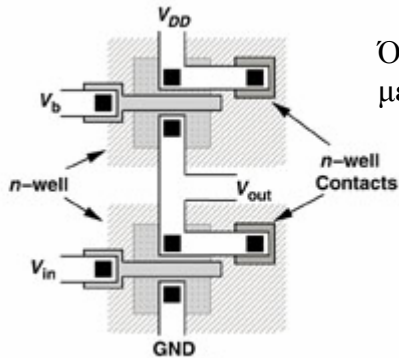


$$A_v \ \lambda \neq 0 \Rightarrow$$

$$A_v = \frac{\frac{1}{g_{mb}} \parallel r_{D1} \parallel r_{D2} \parallel R_L}{\frac{1}{g_{mb}} \parallel r_{D1} \parallel r_{D2} \parallel R_L + \frac{1}{g_m}}$$

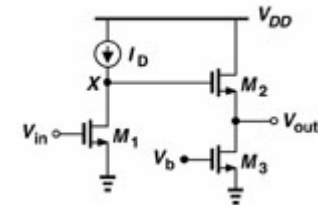


(a)



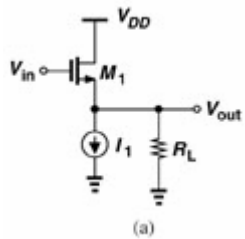
(b)

Όχι φαινόμενο σώματος αλλά μεγαλύτερη αντίσταση εξόδου.

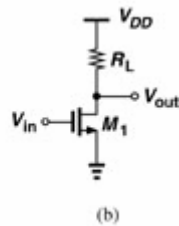


Ολίση της DC τάσης κατά V_{GS} .

$$V_X = V_{GS2} + V_{DS3} \geq V_{GS2} + (V_{GS3} - V_{TH3})$$



(a)



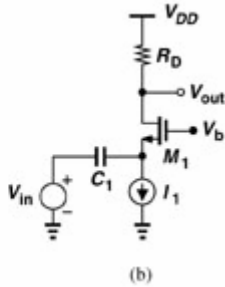
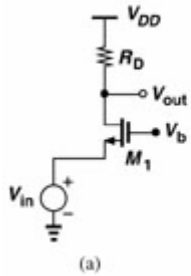
(b)

Η απολαβή για μικρή R_L .

$$\left. \frac{V_{out}}{V_{in}} \right|_{SF} \approx \frac{R_L}{R_L + \frac{1}{g_{m1}}}$$

$$\left. \frac{V_{out}}{V_{in}} \right|_{CS} \approx -g_{m1} R_L$$

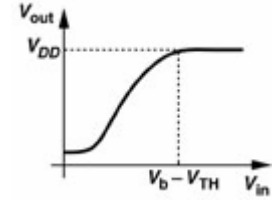
Βαθμίδα Κοινής Πύλης



$$A_v \quad V_{in} \geq V_b - V_{TH} \Rightarrow V_{out} = V_{DD}$$

$$A_v \quad V_{in} < V_b - V_{TH} \Rightarrow I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH})^2$$

$$A_v \quad V_{DD} - \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH})^2 R_D = V_b - V_{TH} \quad \text{τρίοδος}$$



Στον κόρο

$$V_{out} = V_{DD} - \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH})^2 R_D$$

$$\frac{\partial V_{out}}{\partial V_{in}} = -\mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH}) \left(-1 - \frac{\partial V_{TH}}{\partial V_{in}}\right)$$

$$\frac{\partial V_{TH}}{\partial V_{in}} = \frac{\partial V_{TH}}{\partial V_{SB}} = \eta$$

$$\frac{\partial V_{out}}{\partial V_{in}} = \mu_n C_{ox} \frac{W}{L} R_D (V_b - V_{in} - V_{TH})(1 + \eta) = g_m (1 + \eta) R_D$$

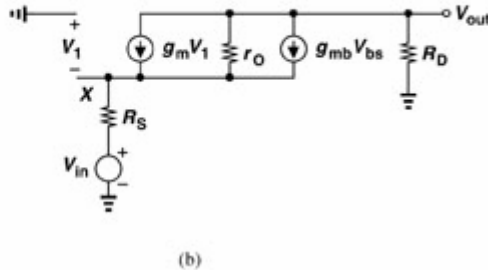
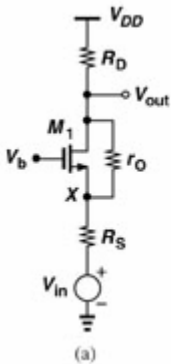
Το φαινόμενο σώματος αυξάνει την απολαβή!

Αντίσταση εισόδου για $\lambda=0$

$$1/(g_m + g_{mb}) = 1/[g_m(1 + \eta)]$$

Το φαινόμενο σώματος μειώνει την αντίσταση εισόδου

Για $\lambda \neq 0$ και $R_s \neq 0$



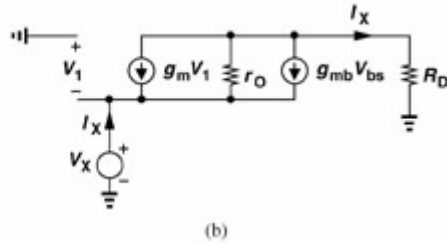
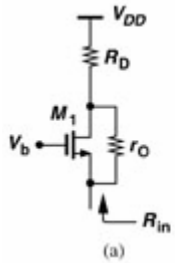
$$V_1 - \frac{V_{out}}{R_D} R_S + V_{in} = 0$$

$$r_D \left(-\frac{V_{out}}{R_D} - g_m V_1 - g_{mb} V_1 \right) - \frac{V_{out}}{R_D} R_S + V_{in} = V_{out}$$

$$r_D \left[-\frac{V_{out}}{R_D} - (g_m + g_{mb}) \left(V_{out} \frac{R_S}{R_D} - V_{in} \right) \right] - \frac{V_{out}}{R_D} R_S + V_{in} = V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{(g_m + g_{mb}) r_D + 1}{r_D + (g_m + g_{mb}) r_D R_S + R_S + R_D} R_D$$

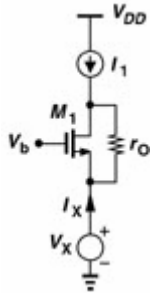
Οι αντιστάσεις εισόδου και εξόδου της τοπολογίας κοινής πύλης



$$R_D I_X + r_D [I_X - (g_m + g_{mb}) V_X] = V_X$$

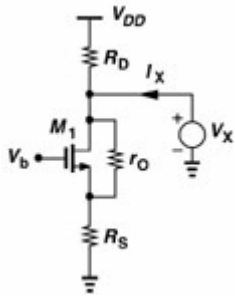
$$R_{in} = \frac{V_X}{I_X} = \frac{R_D + r_D}{1 + (g_m + g_{mb}) r_D} \approx \frac{R_D}{(g_m + g_{mb}) r_D} + \frac{1}{g_m + g_{mb}}$$

$$R_D = 0 \Rightarrow \frac{V_X}{I_X} = \frac{r_D}{1 + (g_m + g_{mb}) r_D} = \frac{1}{\frac{1}{r_D} + g_m + g_{mb}} \quad \text{Όπως στον ακολουθητή πηγής.}$$



$$R_{in} \Rightarrow \infty$$

Άρα, η αντίσταση εισόδου της βαθμίδας κοινής πύλης είναι σχετικά μικρή μόνο αν η R_D είναι μικρή.



$$R_{out} = \{ [1 + (g_m + g_{mb}) r_D] R_S + r_D \} \parallel R_D \quad \text{Όπως στον CS με εκφυλισμό πηγής.}$$

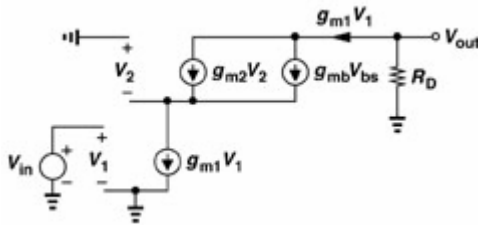
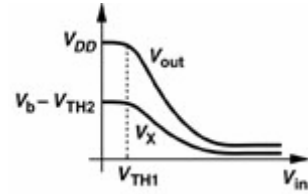
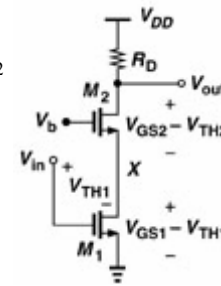
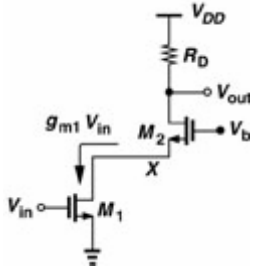
Συνδεσμολογία σειράς (cascode)

Για $V_X \geq V_{in} - V_{TH1} \rightarrow M1$ στον κόρο.

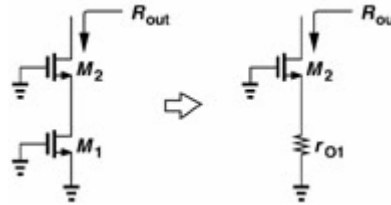
Επειδή $V_X = V_b - V_{GS2} \Rightarrow V_b - V_{GS2} \geq V_{in} - V_{TH1}$ και επομένως $V_b > V_{in} + V_{GS2} - V_{TH1}$.

Για να είναι το $M2$ στον κόρο, πρέπει $V_{out} \geq V_b - V_{TH2} \Rightarrow V_{out} \geq V_{in} - V_{TH1} + V_{GS2} - V_{TH2}$

αν το V_b επιλεγεί έτσι ώστε να τοποθετεί το $M1$ στην αρχή του κόρου.

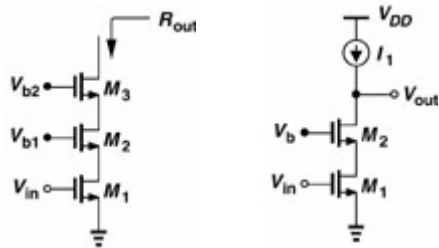


$$A_v \lambda=0 \Rightarrow A_v = A_{vCS}$$



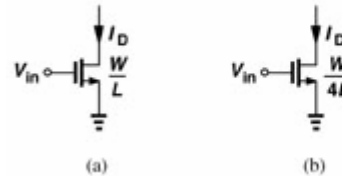
$$R_{out} = [1 + (g_{m2} + g_{mb2})r_{D2}]r_{D1} + r_{D2}$$

Υψηλή αντίσταση εξόδου.

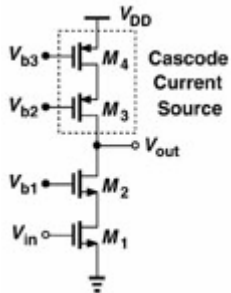


$$G_m \approx g_{m1} \text{ και } R_{out} \approx (g_{m2} + g_{mb2})r_{D2}r_{D1} \Rightarrow$$

$$A_v = (g_{m2} + g_{mb2})r_{D2}g_{m1}r_{D1}$$



$$g_m r_D = \sqrt{2 \frac{W}{L} \mu_n C_{ox} I_D} \frac{1}{\lambda I_D}$$



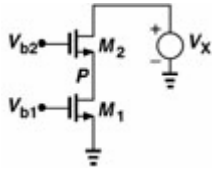
$$V_{DD} - (V_{GS1} - V_{TH1}) - (V_{GS2} - V_{TH2}) - |V_{GS3} - V_{TH3}| - |V_{GS4} - V_{TH4}|$$

$$R_{out} = \{ [1 + (g_{m2} + g_{mb2})r_{D2}]r_{D1} + r_{D2} \} \{ [1 + (g_{m3} + g_{mb3})r_{D3}]r_{D4} + r_{D3} \}$$

$$|A_v| \approx g_{m1} R_{out}$$

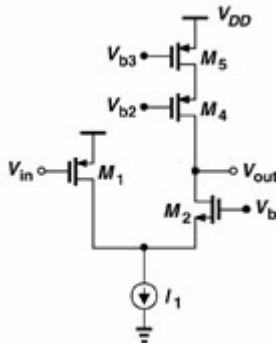
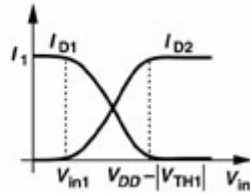
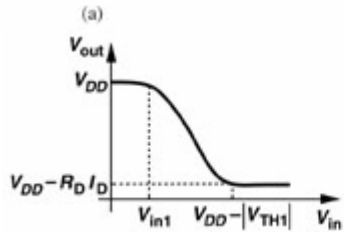
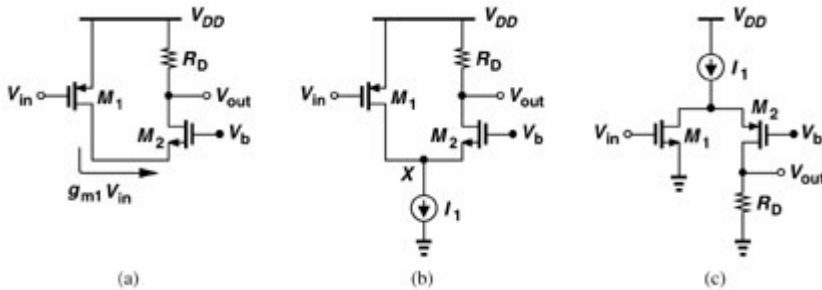
$$|A_v| \approx g_{m1} [(g_{m2} r_{D2} r_{D1}) \parallel (g_{m3} r_{D3} r_{D4})]$$

Ιδιότητα θωράκισης



$$I_{D2} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 [2(V_{b2} - V_p - V_{TH2})(V_x - V_p) - (V_x - V_p)^2]$$

Αναδιπλωμένη συνδεσμολογία σειράς



Για $V_{in} < V_{DD} - |V_{TH1}| \Rightarrow M1$ στον κόρο

$$I_{D2} = I_1 - \frac{1}{2} \mu_p C_{ox} \left(\frac{W}{L}\right)_1 (V_{DD} - V_{in} - |V_{TH1}|)^2$$

Για $V_{in} \ll \Rightarrow I_{D2} = 0$

$$\frac{1}{2} \mu_p C_{ox} \left(\frac{W}{L}\right)_1 (V_{DD} - V_{in} - |V_{TH1}|)^2 = I_1$$

$$V_{in} = V_{DD} - \sqrt{\frac{2I_1}{\mu_p C_{ox} (W/L)_1}} - |V_{TH1}|$$

$$V_{\chi} \rightarrow V_{DD}$$