

Top Down Parsing

- Start at the root of the parse tree and grow toward leaves.
- Pick a production and try to match the input.
- Repeat until the fringe of the parse tree matches the input string.

Grammars and Parsers

LL(1) parsers

- **L**eft-to-right input
- **L**eftmost derivation
- **1** symbol of look-ahead

LL(1) Grammars

- **Def:** a grammar is LL(1) iff

$A \rightarrow \alpha$ and $A \rightarrow \beta$ and

$\text{FIRST}_+(A \rightarrow \alpha) \cap \text{FIRST}_+(A \rightarrow \beta) = \emptyset$

LL(1) grammars are:

- not ambiguous and
- not left-recursive

Example

#	Production rule
1	Tern -> '0'..'9' '?' Tern ':' Tern
2	'0'..'9'

- Problem?
- How do we predict which production to use?

Left factoring

#	Production rule
1	Tern \rightarrow '0'..'9' TernTail
2	TernTail \rightarrow '?' Tern ':' Tern
3	ϵ

FIRST and FOLLOW sets

#	Production rule
1	Tern \rightarrow '0'..'9' TernTail
2	TernTail \rightarrow '?' Tern ':' Tern
3	ϵ

$\text{FIRST}(\#1) = \{ '0' \dots '9' \}$

$\text{FIRST}(\#2) = \{ '?' \}$

$\text{FIRST}(\#3) = \{ '\epsilon' \}$

$\text{FOLLOW}(\text{Tern}) = \{ ':', \text{EOF} \}$

$\text{FOLLOW}(\text{TernTail}) = \text{FOLLOW}(\text{Tern}) = \{ ':', \text{EOF} \}$

FIRST+ sets

#	Production rule
1	Tern -> '0'..'9' TernTail
2	TernTail -> '?' Tern ':' Tern
3	ϵ

$$\text{FIRST}_+(\#1) = \{ '0' \dots '9' \}$$

$$\text{FIRST}_+(\#2) = \{ '?' \}$$

$$\begin{aligned} \text{FIRST}_+(\#3) = \\ \text{FIRST}(\#3) \cup \text{FOLLOW}(\text{TernTail}) = \\ \{ e, ':', \text{EOF} \} \end{aligned}$$

Table-driven approach

	'0' .. '9'	':'	'?'	EOF
Tern	'0'..'9' TernTail	error	error	error
TernTail	error	ϵ	'?' Tern ':' Tern	ϵ

Recursive descent

- Define a function for each nonterminal.
- Have these functions call each other based on the lookahead token.
- The term *descent* refers to the direction in which the parse tree is built.