

Publish/Subscribe Systems with Distributed Hash Tables and Languages from DHTs

[Extended Abstract]*

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1 Introduction

We consider the problem of implementing *publish/subscribe (pub/sub)* [3] on top of distributed hash tables (DHTs) such as Chord [11]. In publish/subscribe systems, clients post *continuous queries* (or *subscriptions*) to receive notifications whenever certain *resources* of interest are *published*. There has been lots of work in the area of pub/sub systems concentrating mostly on algorithms for the *problem*: If Q is the set of queries posted to the network and p is a published resource, how do we find efficiently which queries $q \in Q$ match p ?

This work presents DH_Trie, a distributed algorithm that uses a Chord protocol to distribute queries to super-peers and a *forest of tries* to index queries at each super-peer. These data structures are used to solve the problem efficiently. Our work adopts the super-peer architecture and languages of P2P-DIET [8, 6]. Thus our pub/sub network has two kinds of nodes: *super-peers* and *clients*. All super-peers are equal and have the same responsibilities, thus the super-peer subnetwork is a *pure* P2P network. Each super-peer serves a fraction of the clients. It is very easy to modify our proposal to the case of pure P2P networks where all nodes are equal. The fundamental difference of this work and our previous work on P2P-DIET is that DH_Trie is based on ideas from distributed hash tables.

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We use the data model \mathcal{AWP} of P2P-DIET for specifying queries and source meta-data. \mathcal{AWP} is based on concepts from Information Retrieval and the concept of *attribute* with values of type *text* [9]. To the best of our knowledge, this is the first paper that discusses how to implement pub/sub systems using IR-based languages using ideas from DHTs. Other interesting work in this area which adopts different data models includes [10, 12].

The rest of this extended abstract is organised as follows. Section 3 describes the distributed algorithm DH \mathcal{T} rie. Section 4 briefly describes algorithm BestFit \mathcal{T} rie that is the local component of DH \mathcal{T} rie run by each super-peer and summarises our experimental evaluation of BestFit \mathcal{T} rie. Finally, Section 5 discusses future work and progress.

2 The Data Model \mathcal{AWP}

In [9] we presented the data model \mathcal{AWP} for specifying queries and source meta-data. We give here a brief description of the main concepts of \mathcal{AWP} since it is the data model used in the rest of the paper. \mathcal{AWP} is based on the concept of *attributes* with values of type *text*. The query language of \mathcal{AWP} uses *Boolean* and *proximity operators* on attribute values as in the work of [10]. \mathcal{AWP} is based on the Boolean model of IR.

Let Σ be a finite *alphabet*. A *word* is a finite non-empty sequence of characters from Σ . Let \mathcal{A} be a countably infinite set of attributes called the *attribute set*. In practice attributes will come from *namespaces* appropriate for the application at hand e.g., from the set of Dublin Core Metadata Elements². If $A \in \mathcal{A}$ denotes a set of words called the *vocabulary* of attribute A . A *text value* s over a vocabulary \mathcal{V} is a total function $s : \{1, 2, \dots, n\} \rightarrow \mathcal{V}$.

A *publication* n is a set of attribute-value pairs (A, s) where $A \in \mathcal{A}$, s is a text value over \mathcal{V}_A , and all attributes are *distinct*. The following is a publication:

$$\begin{aligned} & \{ (AUTHOR, \text{"John Smith"}), \\ & (TITLE, \text{"Information dissemination in P2P systems"}), \\ & (ABSTRACT, \text{"In this paper we show that ..."}) \} \end{aligned}$$

A *query* is a conjunction of atomic formulas of the form $A = s$ or $A \supseteq wp$ where wp is a word pattern containing conjunction of words and proximity operators. Atomic formulas with only words as subformulas. The following is an example of a query under \mathcal{AWP} :

$$\begin{aligned} & (AUTHOR = \text{"John Smith"}) \wedge \\ & (TITLE \supseteq (\text{peer-to-peer} \wedge (\text{selective} \prec_{[0,0]} \text{dissemination} \prec_{[0,3]} \text{information}))) \end{aligned}$$

The above query requests all resources that have *John Smith* as their author and their title contains the word *peer-to-peer* and a word pattern where the word *selective* is immediately followed by the word *dissemination* which in turn is followed by the word *information* after at most three words.

²<http://purl.org/dc/elements/1.1/>

3 The Algorithm DHTriE

DHTrie uses *three levels of indexing* to store continuous queries submitted by clients. The first level corresponds to the partitioning of the global query space into different super-peers using DHTs as the underlying infrastructure. Each super-peer is responsible for a fraction of the submitted user queries through a mapping of attribute-value combinations to super-peer identifiers. The distributed DHT infrastructure is used to define the mapping scheme and also manage the routing of messages between different super-peers.

The other two levels of our indexing mechanism are managed by different sets of the super-peers, as they are used for indexing the user queries that are submitted to a super-peer responsible for. In the second level each super-peer uses a hash table to index the user queries by attributes contained in a query, whereas in the third level a trie-like structure where the mapping scheme exploits commonalities between atomic queries is utilised.

3.1 Mapping Keys to Super-Peers

We use a Chord-like DHT to implement our super-peer network. Chord uses consistent hashing to map keys to nodes. Each node and data item is assigned a unique k bit identifier, where k is the length of an identifier that should be large enough to avoid the possibility of different items hashing to the same identifier. Identifiers can be thought of as being placed on a circle from 0 to $2^k - 1$, called the *Chord circle* or *Chord ring*. If H is the hash function used, then data item r is stored at the node with identifier $H(r)$ if this node exists. Alternatively, r is stored at the node whose identifier is the first identifier *clockwise* in the Chord ring starting from $H(r)$. This node is called the *successor* of node $H(r)$ and is denoted by $successor(H(r))$. We will say that this node is *responsible* for data item r .

3.2 Subscribing With a Continuous Query

Let us assume that a client C wants to submit a continuous query q of the form

$$A_1 = s_1 \wedge \dots \wedge A_m = s_m \wedge A_{m+1} \supseteq wp_{m+1} \wedge \dots \wedge A_n \supseteq wp_n$$

C contacts a super-peer S (its *access point*) and sends it a SUBMITCQUERY message, where $id(C)$ is a unique identifier assigned to C by S in this communication. When S receives q , it selects a random attribute A_i , $1 \leq i \leq m$, contained in q and a random word w_j from text value s_i or word pattern wp_j (depending on what kind of atomic formula of query q attribute A_i appears in). Then S forms the concatenation $A_i w_j$ of strings A_i and w_j and computes $H(A_i w_j)$ to obtain a super-peer identifier. Finally, S creates FWDCQUERY($id(S)$, $A_i w_j$) message and forwards it to super-peer with identifier $H(A_i w_j)$ using the underlying infrastructure of the DHT.

When a super-peer receives a FWDCQUERY message containing q , q in its local data structures using the insertion algorithm of BestFitTrie described briefly in Section 4 and also in [13, 7].

3.3 Publishing a Resource

When client C wants to publish a resource, it constructs a publication p of the form $\{(A_1, s_1), (A_2, s_2), \dots, (A_n, s_n)\}$, it contacts a super-peer S and sends S a SOURCE($id(C), p$) message. When S receives p , it computes a list of super-peer identifiers that are provably a superset of the set of super-peer identifiers suitable for queries that match p . This list is computed as follows. For every attribute A_i , $1 \leq i \leq n$ in p , and every word w_j in s_i , S computes $H(A_i w_j)$ to obtain a list of super-peer identifiers that, according to the DHT mapping function, store continuous queries containing word w_j in the respective text value s_i or word w_j in the respective text value s_i . S then sorts this list in ascending order starting from the smallest identifier to obtain list L and creates a FWDRESOURCE($id(S), id(p), p, L$) message. $id(p)$ is a unique metadata identifier assigned to p by S , and sends it to super-peer S' with identifier equal to $head(L)$. This forwarding is done as follows: FWDRESOURCE is sent to a super-peer S' , where $id(S')$ is the greatest identifier in the finger table of S , for which $id(S') \leq head(L)$ holds.

Upon reception of a FWDRESOURCE message by a super-peer S , S checks if $id(S) = head(L)$. If $id(S) = head(L)$ then S removes $head(L)$ from list L and makes a copy of the message. The publication part of this message is then matched against the super-peer's local query database and subscribers are notified (the details of which are presented in Section 3.4). Finally, S forwards the message to super-peer S' with identifier $head(L)$. If $id(S)$ is not in L , then it just forwards the message to S' as described in the previous paragraph.

3.4 Notifying Interested Subscribers

Let us now examine how notifications about published resources are sent to interested subscribers. When a FWDRESOURCE message containing a publication p of a resource arrives at a super-peer S , the continuous queries matching p are found by utilising its local index structures and using the algorithm described briefly in Section 4 and also in [13, 7].

Once all the matching queries have been retrieved from the database, S sends a notification message of the form CQNOTIFICATION($id(C), l(r), L, T$) to the super-peers. $l(r)$ is a link to the resource, L is a list of identifiers of the super-peers intended recipients of the notification message, and T is a list containing the identifiers of the queries that matched p . List L is created as follows. S identifies the super-peers that have at least one client with a query q satisfied by p . The list is sorted in ascending order starting from $id(S)$ and removes duplicate entries. The notification message is then forwarded according to the algorithm described

Id	Query $A_i \sqsupseteq wp_i$	Identifying Subsets
0	$A_i \sqsupseteq \text{databases}$	{databases}
1	$A_i \sqsupseteq \text{relational } \prec_{[0,2]} \text{ databases}$	{databases, relational}
2	$A_i \sqsupseteq \text{databases} \wedge \text{relational}$	{databases, relational}
3	$B_i \sqsupseteq (\text{software } \prec_{[0,2]} \text{ neural } \prec_{[0,0]} \text{ networks}) \wedge (\text{software } \prec_{[0,3]} \text{ relational } \prec_{[0,0]} \text{ databases})$	{databases, relational, neural}, ...
4	$A_i \sqsupseteq \text{optimal} \wedge (\text{artificial } \prec_{[0,0]} \text{ intelligence}) \wedge \text{relational} \wedge \text{databases}$	{databases, relational, artificial, intelligence, optimal}, ...
5	$A_i \sqsupseteq \text{artificial} \wedge \text{relational} \wedge \text{intelligence} \wedge \text{databases} \wedge \text{knowledge}$	{databases, relational, artificial, intelligence, knowledge}, ...

Table 1: Identifying subsets of $words(wp_i)$ with respect to $S = \{words(wp_i) \mid i \in \{0, \dots, 5\}\}$.

Section 3.3.

Upon arrival of a CQNOTIFICATION message at a super-peer S , $head(L)$ is checked to find out whether S is an intended recipient of the message. If S is, S just forwards the message to another super-peer using information from T and the algorithm described in Section 3.3. If $head(L) = id(S)$, S scans T to find the set U of query identifiers that belong to clients that have their access point, by utilising a hash table that associates query identifier with client identifiers. For each distinct query identifier in set U , a MATCHSOURCE($id(S), id(q), l(r)$) message is created and forwarded to the appropriate client. Finally S removes $head(L)$ from L and U from T , and forwards CQNOTIFICATION message according to the algorithm described in Section 3.3.

4 Local Algorithms and Data Structures

In this section we describe the indexing structures that are used locally by each super-peer to store the continuous queries it is responsible for. These structures are utilised in the step of DHtrie described in Section 3.4 to efficiently which queries match a given publication.

4.1 The Algorithm BestFitTrie

To index queries BestFitTrie utilises an array, called the *attribute directory*, that stores pointers to word directories. AD has one element for each distinct attribute in the query database. For a query of the form presented in Section 3.1,

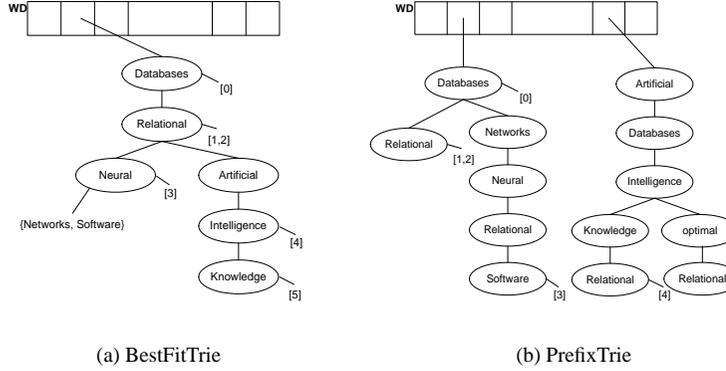


Figure 1: Organisation of the atomic queries of Table 1

word directory $WD(A_i)$, $m + 1 \leq i \leq n$ is a hash table that provides fast access to the roots of tries in a forest that is used to organize sets of words – the set of words in wp_i for each atomic formula $A_i \sqsupseteq wp_i$ in a query (denoted by wor). The proximity formulas contained in each wp_i are stored in an array called proximity array (PA). PA stores pointers to trie nodes (words) that are contained in proximity formulas along with the respective proximity intervals for each formula. There is also a hash table, called equality table (ET), that indexes values s_j , $1 \leq j \leq m$ that appear in atomic formulas of the form $A_j = s_j$. The idea behind BestFitTrie is to identify common parts between queries (through the use of identifying subsets; an example is shown in Table 1) and to exploit these commonalities to achieve faster filtering. BestFitTrie is described in detail in [14].

To evaluate the performance of BestFitTrie we have also implemented three algorithms: BF, SWIN and PrefixTrie. BF (Brute Force) has no indexing structure and scans the query database sequentially to determine matching queries. SWIN (Single Word INdex) utilises a two-level index for accessing queries in an efficient way. A query of the form presented at Section 3.2, is indexed by SWIN under its attributes A_1, \dots, A_n and also under m text values s_1, \dots, s_m and $n - m$ words selected randomly from wp_{m+1}, \dots, wp_n . More specifically SWIN utilises SWIN to index equalities and an AD pointing to several WDs to index the atomic queries. Atomic queries within a WD slot are stored in a list. PrefixTrie is an extension of the algorithm Tree of [14] appropriately modified to capture attributes and proximity information. Tree was originally proposed for indexing conjunctions of keywords in secondary storage in the context of the SD algorithm SIFT. Following Tree, PrefixTrie uses sequences of words sorted in lexicographic order for capturing the words appearing in the word patterns of atomic queries (instead of sets used by BestFitTrie). A trie is then used to store se

compactly by exploiting *common prefixes* [14].

Algorithm BestFitTrie constitutes an improvement over PrefixTrie. PrefixTrie examines only the prefixes of sequences of words in lexicographic order to identify common parts, it misses many opportunities for clustering. Figure 1(b) where the trie constructed by PrefixTrie for the example query (Table 1 is shown). BestFitTrie keeps the main idea behind PrefixTrie but bundles the words contained in a query as a set rather than as a sorted sequence (ii) searches exhaustively the forest of tries to discover the best place to insert a new set of words. This allows BestFitTrie to achieve better clustering as shown in Figure 1, where we can see that it needs only one trie to store the set of words for the formulas of Table 1, whereas PrefixTrie introduces redundant nodes. These are the result of using a lexicographic order to identify common parts. This redundancy can be the cause of deceleration of the filtering process as we will show in the next section. To improve beyond BestFitTrie it would be interesting to consider *re-organizing* the word directory every time a new set of words arrives, or periodically, but this might turn out to be prohibitively expensive. The work we have not explored this approach in any depth.

4.2 Experimental Evaluation

To evaluate the performance of our local indexing structures we used sequences of documents downloaded from ResearchIndex³ and originally compiled in the NN corpus. Documents are research papers in the area of Neural Networks and we view them as the NN corpus. Because no database of queries was available we developed a methodology for creating user queries using *words* and *terms* (phrases) extracted automatically from the Research Index documents using the C-value/NC-value approach of [5].

All the algorithms were implemented in C/C++, and the experiments were run on a PC, with a Pentium III 1.7GHz processor, with 1GB RAM, Linux. The results of each experiment are averaged over 10 runs to eliminate fluctuations in the time measurements.

The first experiment that we conducted to evaluate BestFitTrie targeted its performance under different sizes of the query database. In this experiment we randomly selected one hundred documents from the NN corpus and used them as incoming documents in query databases of different sizes. The size of the matching percentage for each document used was different, but the average document size was 6869 words, whereas on average 1% of the queries stored in the database were the incoming documents.

As we can see in Figure 2, the time taken by each algorithm grows exponentially with the size of the query database. However SWIN, PrefixTrie and BestFitTrie are less sensitive than Brute Force to changes in the query database size.

³<http://www.researchindex.com>

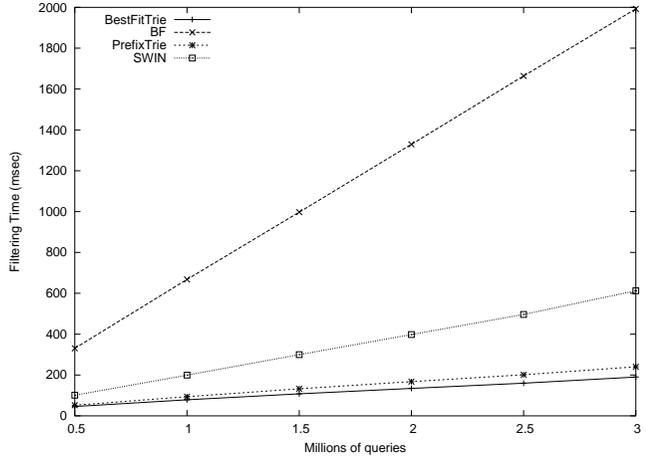


Figure 2: Effect of the query database size in filtering time

trie-based algorithms outperform SWIN mainly due to the clustering technique that allows the exclusion of more non-matching atomic queries during filtering. We can also observe that the better exploitation of the commonalities among queries improves the performance of BestFitTrie over PrefixTrie, resulting in a significant speedup in filtering time for *large query databases* (BestFitTrie is 100% faster than PrefixTrie and 1000% faster than sequential scan for a database of 3 million queries). Additionally, Figure 3 contrasts the algorithms in terms of insertion time. In this figure we can see the average time in milliseconds to insert a new query in a query database of different sizes. Notice that in a database of 2.5 millions of queries BestFitTrie needs 5 milliseconds more to insert a new query into the database, to save about 45 milliseconds at filtering time.

Comparison of the algorithms in terms of throughput results in BestFitTrie giving the best filtering performance managing to process a load of about 100 queries per second (about 9 ResearchIndex papers) per second for a query database of 3 million queries.

In terms of space requirements BF needs about 15% less space than the other trie-based algorithms, due to the simple data structure that poses small space requirements. Additionally the rate of increase for the two trie-based algorithms is similar to that of BF, requiring a fixed amount of extra space each time. From the experiments above it is clear that BestFitTrie speeds up the filtering process without extra storage cost, and proves faster than the rest of the algorithms, managing to filter as much as 3 million queries in less than 200 milliseconds, which is 1000 times faster than the sequential scan method.

We have also evaluated the performance of the algorithms under two different parameters: *document size* and *percentage of queries matching a publisher*.

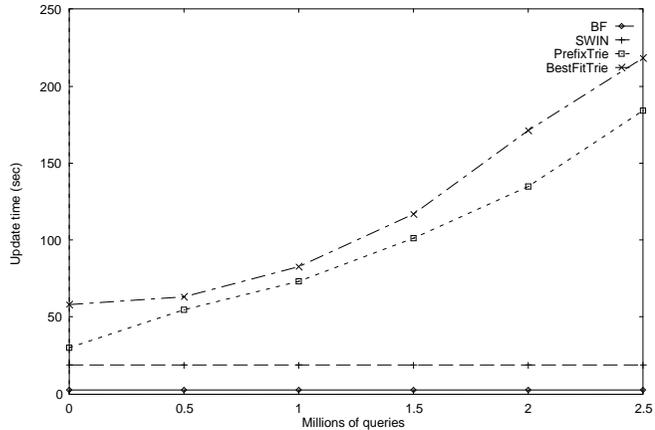


Figure 3: Query insertion time for different query database sizes

ment. Document size does not appear to significantly affect trie-based algorithms, mainly due to the data structures used for the representation of an incoming document and the way the matching process is carried out. On the other hand, the percentage of the stored queries that match an incoming document seems to have less effect on SWIN. In this experiment BestFitTrie seemed more sensitive to PrefixTrie to the matching percentage, but still proved more efficient in terms of filtering time and throughput.

Finally we have developed various heuristics for ordering words in the tries maintained by PrefixTrie and BestFitTrie when *word frequency* information (or *word ranking*) is available, as it is common in IR research [2]. Using the *rank* heuristic (*irank*) [14], we store the least frequent words of the queries at the roots of the tries, while the frequent ones are pushed deeper in the tries, resulting in many narrow tries. Thus more queries are put in subtrees containing words occurring less frequently, resulting in less lookups during filtering time. The algorithms using the *irank* heuristic are PrefixTrie-*irank* and BestFitTrie-*irank*. The faster algorithm is shown to be a variation of BestFitTrie, called LCWTr (Least Common Word), where BestFitTrie is limited to consider a single candidate during query insertion: the one that has the least frequent word of the atom as root. The details of the experiments briefly mentioned above are presented in detail in [13].

5 Work in Progress

Performance evaluation in the distributed case. To evaluate the performance and scalability of DHTrie we are currently implementing the algorithms

tion 3. We plan to evaluate DH_Trie by considering its behaviour (mainly in terms of message load between super-peers) under various parameters and resource size, arrival rates of queries and resources, number of super-peers etc.). Furthermore we plan to extend the algorithm to take locality into account by maintaining extra routing tables for the most frequently accessed super-peers (namely the super-peers responsible for the most frequently published).

Load balancing. A key problem that arises when trying to partition the space among the different super-peers in our overlay network is *load balancing*. The idea here is to avoid having overloaded peers i.e., peers having to handle a great number of posted queries (this is what [1] calls *storage load balancing* although the paper [1] is not in a pub/sub setting, the concept is the same).

In addition, we would like to have a way to deal with the load balancing problem posed to super-peers that are responsible for pairs (A, w) , where w occurs frequently in text values involving A . We expect the frequency of occurrence of words appearing in a query within an atomic formula with attribute A to have a non-uniform distribution (e.g., a skewed distribution like the Zipf distribution [15]). We do not know of any study that has shown this by examining collections of user queries; however, such an assumption seems intuitive especially in the light of similar distributions of words in text collections [2]. As an example in a digital library application we would expect distinguished author names to occur frequently in queries with the AUTHOR attribute, or popular topics to appear frequently in queries with the TITLE attribute. Thus in our case, uniformity of items (i.e., queries) as traditionally assumed by DHTs is not applicable.

We are currently working on addressing the above load balancing problem by utilizing ideas from the algorithm LCW_Trie described in detail in [13], where queries are indexed under infrequent words; we also use a form of content replication to deal with overloading due to notification processing. It would be interesting to compare this approach to what is advocated in [1].

Word frequency computation in a distributed setting. Computing the frequency of occurrence of words in a distributed setting is a crucial problem if one wants to support vector space queries or to provide for load balancing among super-peers as showed above. There are mainly two approaches to the word frequency computation in a distributed setting; (a) a global ranking scheme that assumes the existence of a central authority that maintains the frequency information or a message-intensive distributed mechanism that notifies every peer in the network about changes in frequency information or (b) a local ranking scheme that computes word frequencies p_i based solely on frequencies of words in documents that are published. It is clear that the first approach affects the scalability and efficiency of the system while the second approach can be misleading due to peer specialisation.

In related work we present a distributed word ranking algorithm that combines the hybrid form of the two approaches described earlier. It provides an algorithm that is based on local information, but also tries to combine this information

global “truth” through an updating and estimation mechanism.

Reducing network traffic. We can reduce network traffic by *compressing* publications. In the full version of the paper we describe a gap compression technique that allows the matching of a compressed publication against a database of queries using algorithm BestFitTrie.

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