

OPTIMAL TASK ASSIGNMENT IN SENSOR NETWORKS

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MOTIVATION

- In-network processing paradigm
- Millions of sensors with processing capabilities
- Vision
 - Reduce the volume of data seen / processed by the application
- Complex application tasks can split into simpler tasks that can be accomplished by separate nodes within the network
- Goal: assign the tasks optimally in terms of energy
 - Sensing
 - Processing
 - Communication
 - ...



PROBLEM DEFINITION

- Definition (Optimal Assignment)

Let W be a WSN and let T be a complex task. Given the set of all mappings $\Phi = \{\phi: T \rightarrow W\}$ where the capabilities of the network fulfill the task and energy requirements, we call an assignment as **energy-optimal assignment** ϕ_{opt} if and only if

$$(\forall \phi \in \Phi) \varepsilon_{W,T}^{\phi_{opt}} \leq \varepsilon_{W,T}^{\phi} .$$

- NP-hard [Garey and Johnson, 1979]



MODELING FRAMEWORK

Task Model

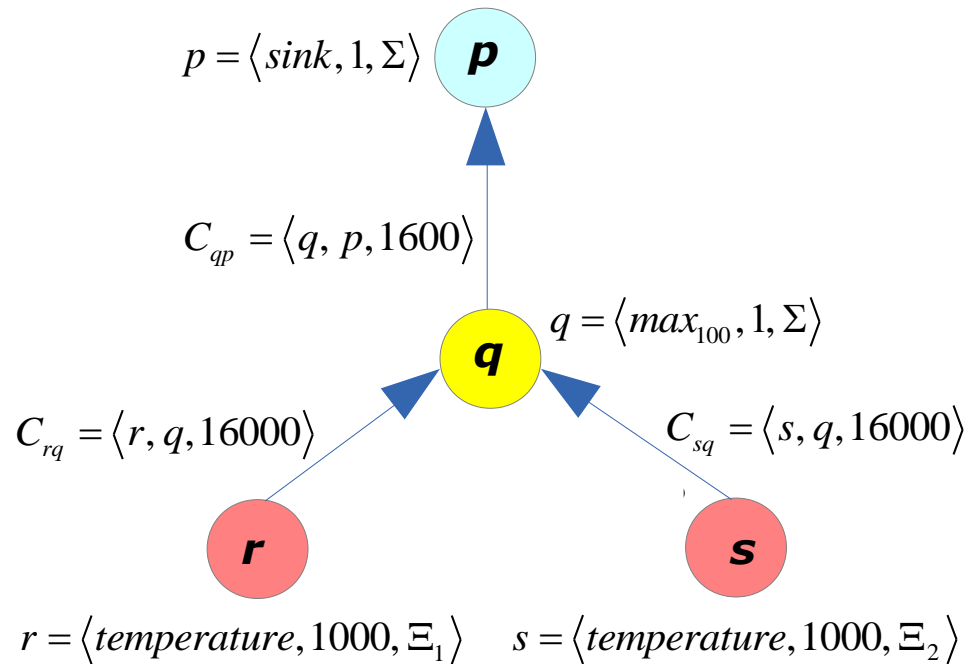
Definition (Task). Given a set S of subtask vertices and a set C of directed edges among the subtask vertices, we define a task T as a *directed acyclic graph (DAG)* represented by the tuple $T \equiv \langle S, C \rangle$.

Category	Description	Input From	Output To
Sensing	Sense context from the environment	-	<ul style="list-style-type: none">• Processing• Sink
Processing	Process input data and forward results	<ul style="list-style-type: none">• Processing• Sensing	<ul style="list-style-type: none">• Processing• Sink
Sink	Retrieve final format of data sensed and processed	<ul style="list-style-type: none">• Processing• Sensing	-



MODELING FRAMEWORK

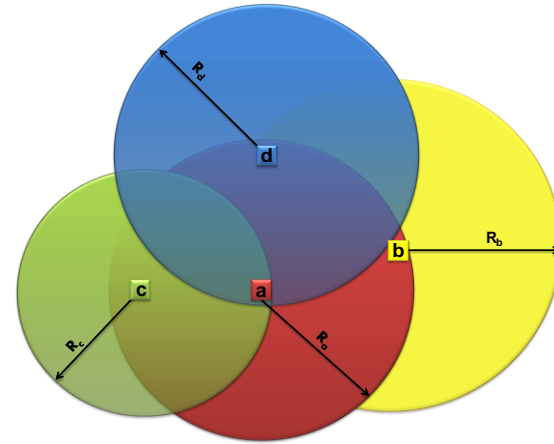
Task Model - Example



MODELING FRAMEWORK

Network Model

Definition (Network). Let N be a set of network nodes and let A be a set of directed network edges. We define a WSN as a *strongly connected directed graph* represented by the tuple $W \equiv \langle N, A \rangle$.



Capability	Sink node	Non-sink node
$Sens_a$	$\{ci_i \in CI\}$	$\{ci_i \in CI\}$
Alg_a	$\{alg_i \in Alg\}$	$\{alg_i \in Alg\}$
$isSink_a$	$\{sink\}$	\emptyset
Op_a	$\{ci_i \in CI\} \cup \{alg_i \in Alg\} \cup \{sink\}$	$\{ci_i \in CI\} \cup \{alg_i \in Alg\}$
Loc_a	$\vec{x}_a \in \Sigma$	$\vec{x}_a \in \Sigma$



MODELING FRAMEWORK

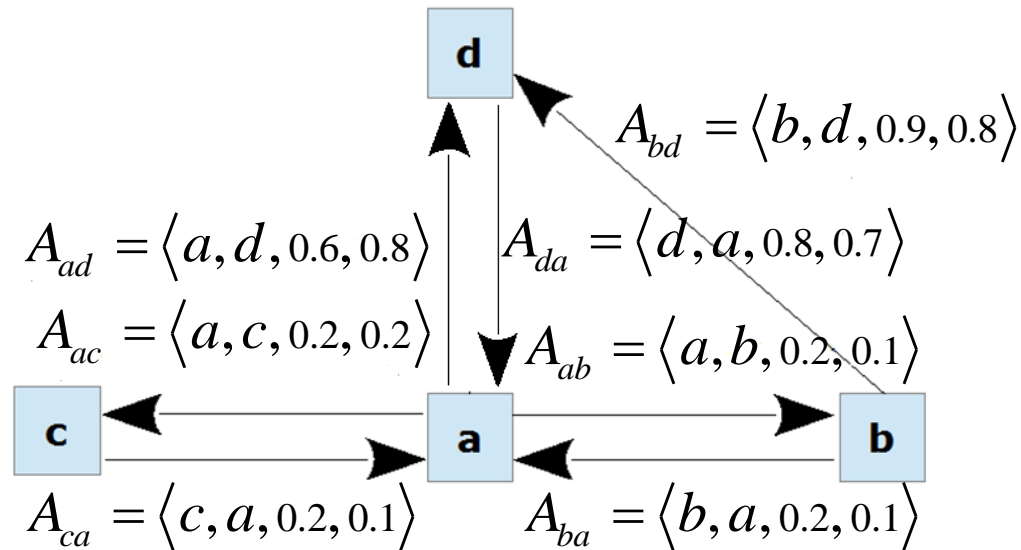
Network Model - Example

$$a = \langle \{ \text{humidity, max} \}, \vec{x}_4, 38000, \{ M_a(\text{humidity}) = 0.001, M_a(\text{max}) = 0.01 \} \rangle$$

$$b = \langle \{ \text{temperature, max} \}, \vec{x}_3, 50000, \{ M_b(\text{temperature}) = 0.002, M_b(\text{max}) = 0.005 \} \rangle$$

$$c = \langle \{ \text{temperature, max} \}, \vec{x}_1, 10800, \{ M_c(\text{temperature}) = 0.001, M_c(\text{max}) = 0.01 \} \rangle$$

$$d = \langle \{ \text{sink, temperature} \}, \vec{x}_2, \infty, \{ M_d(\text{sink}) = 0, M_d(\text{temperature}) = 0.002 \} \rangle$$



MODELING FRAMEWORK

Assignment Model

Definition (Assignment). Let $T \equiv \langle S, C \rangle$ be a complex task and $W \equiv \langle N, A \rangle$ be a WSN with $\Pi = \{\Pi_{ab}\}, \forall a, b \in N$ representing the set of all paths among the network nodes. We define the assignment $\zeta : T \rightarrow W$ as the pair of mappings $X_\zeta : S \rightarrow N$ and $Y_\zeta : C \rightarrow \Pi$ that satisfy the *consistency constraint*:

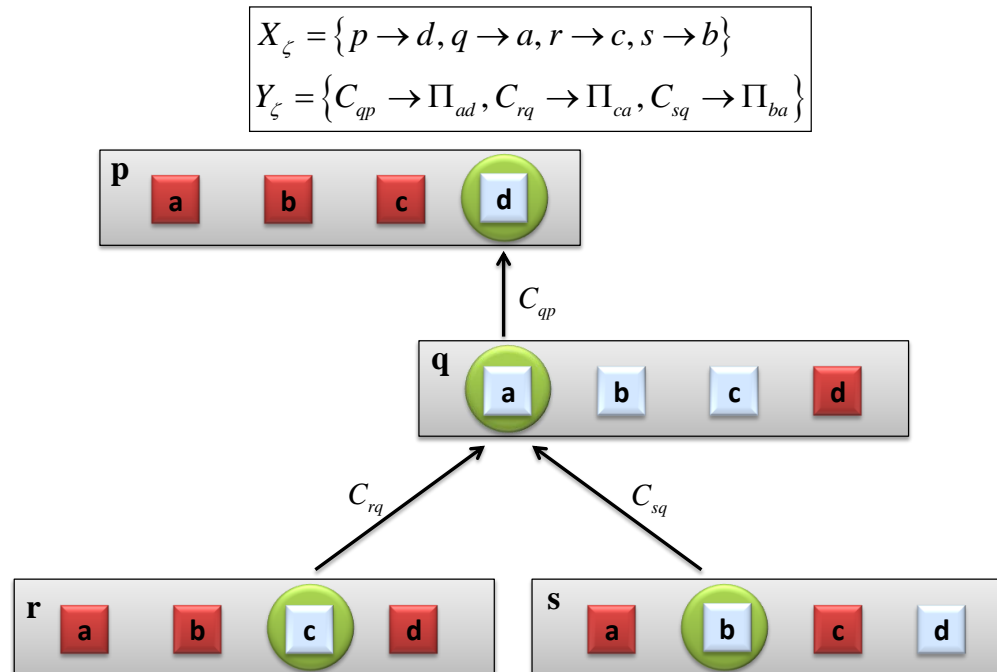
$$\begin{aligned} & \left(\forall C_{pq} \in C \right) \left(\forall \Pi_{ab} \in \Pi \right) Y_\zeta \left(C_{pq} \right) = \Pi_{ab} \Leftrightarrow \\ & \left(\left(X_\zeta \left(p \right) = \text{Src} \left(\Pi_{ab} \right) \right) \wedge \left(X_\zeta \left(q \right) = \text{Dst} \left(\Pi_{ab} \right) \right) \right) \end{aligned}$$

and we represent it by $\zeta \equiv \langle X_\zeta, Y_\zeta \rangle \in Z$ where Z is the set of all possible assignments between T and W .



MODELING FRAMEWORK

Assignment Model - Example



OPTIMIZATION

ILP Variables

Symbol	Type	Size	Description
$x_{p,a}$	Binary Matrix	$ S \cdot N $	Vertex assignment of subtask vertex $p \in S$ to network node $a \in N$
$y_{pq,ab}$	Binary Matrix	$\left(\frac{ S \cdot (S - 1)}{2}\right) \times N ^2$	Edge assignment of subtask edge C_{pq} to network path Π_{ab}
β_{pq}	Integer Column	$\frac{ S \cdot (S - 1)}{2}$	Data bits exchanged over subtask edge C_{pq}
ρ_{ab}	Real Column	$ N ^2$	Total energy rate (per bit) when the network path Π_{ab} is activated
$\rho_{ab,c}$	Real Matrix	$ N ^3$	Energy rate (per bit) for network node $c \in N$ when network path Π_{ab} is activated
$\varepsilon_{c,p}$	Real Column	$ S \cdot N $	Execution energy cost of subtask vertex $p \in S$ in network node $c \in N$
ε_c	Real Column	$ N $	Available energy of network node $c \in N$



OPTIMIZATION

ALGORITHM 1. ILP Formulation

Input: Sets $C, S, N, \Pi, I_p, J_{pq}$, Variables $\beta_{pq}, \rho_{ab}, \rho_{ab,c}, \varepsilon_{c,p}, \varepsilon_c$

Output: Variables $x_{p,a}, y_{pq,ab}$

Objective function: minimize $\left\{ \sum_{c \in N} \left(\sum_{p \in S} \varepsilon_{c,p} \cdot x_{p,c} + \sum_{C_{pq} \in C} \sum_{\Pi_{ab} \in \Pi} \beta_{pq} \cdot y_{pq,ab} \cdot \rho_{ab,c} \right) \right\}$

Constraints set:

$(\forall p \in S) \sum_{a \in N} x_{p,a} = 1$ //Unique subtask vertex assignment constraint

$(\forall C_{pq} \in C) \sum_{\Pi_{ab} \in \Pi} y_{pq,ab} = 1$ //Unique subtask edge assignment constraint

$(\forall C_{pq} \in C)(\forall a \in N) \sum_{\Pi_{ab} \in Src(a)} y_{pq,ab} = x_{p,a}$ //Edge-to-source-vertex consistency

constraint

$(\forall C_{pq} \in C)(\forall b \in N) \sum_{\Pi_{ab} \in Dst(b)} y_{pq,ab} = x_{q,b}$ //Edge-to-destination-vertex consistency

constraint

$(\forall c \in N) \sum_{p \in S} \varepsilon_{c,p} \cdot x_{p,c} + \left\{ \sum_{C_{pq} \in C} \sum_{\Pi_{ab} \in \Pi} \beta_{pq} \cdot y_{pq,ab} \cdot \rho_{ab,c} \right\} \leq \varepsilon_c$ //Node energy conservation

constraint

$(\forall p \in S)(\forall a \in N / I_p) x_{p,a} = 0$ //Vertex compatibility constraint

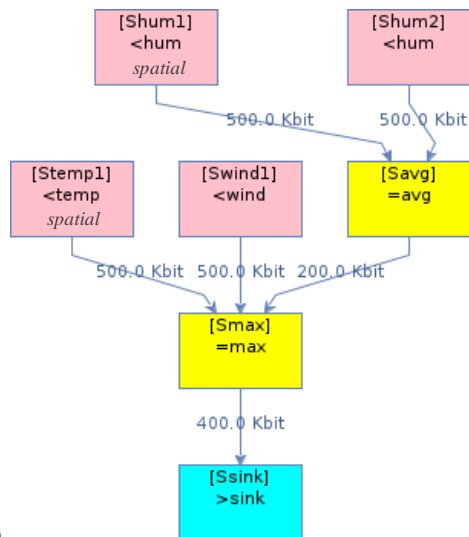
$(\forall C_{pq} \in C)(\forall \Pi_{ab} \in \Pi \setminus J_{pq}) y_{pq,ab} = 0$ //Edge compatibility constraint



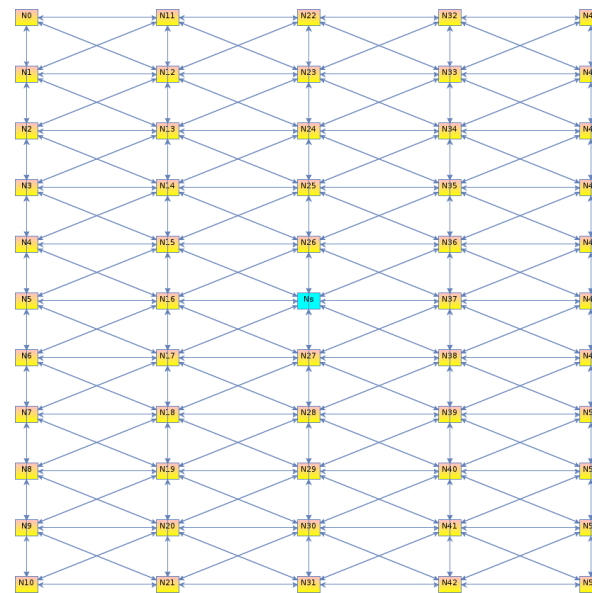
RESULTS

Experimental setting

Parameter	Value
$ CI $	10
$ Alg $	15
$ Sens_{aver} $	4
$ Alg_{aver} $	2
$Quant_{aver}$	6000
#SinkSubtasks	1
$\beta_{pq,aver}$	320 Kbit
<i>Spatial constraint</i>	1:5 sensing subtasks



Parameter	Value
$ Sens_{aver} $	5
$ Alg_{aver} $	10
#SinkNodes	1
$M_{aver}(op_i)$	0.005mJ
$\rho_{trx,aver} = \rho_{rcv,aver} = \rho_{aver}$	0.0001mJ/bit
ϵ_{aver}	300J



Optimal Task Assignment in Sensor Networks



RESULTS

Energy status of the network after Run #100

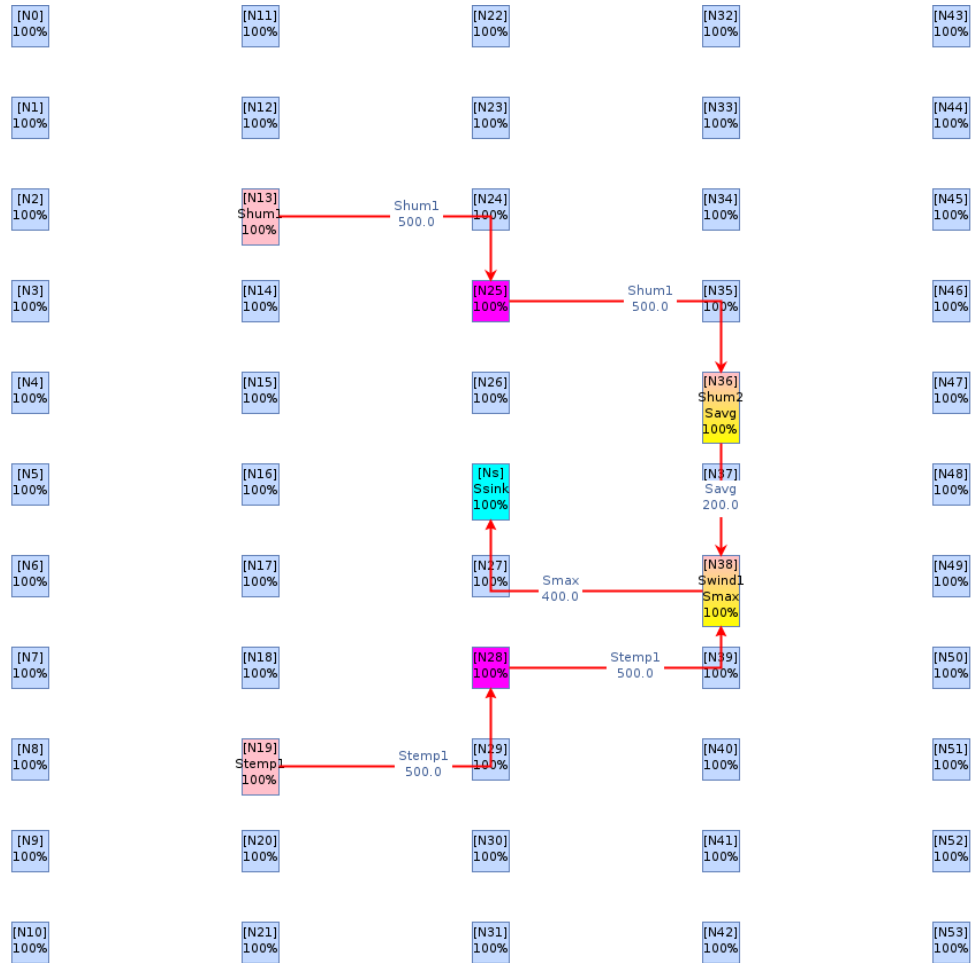
N0	N21	N42	N63	N84	N105	N126	N147	N168	N189	N210	N230	N251	N272	N293	N314	N335	N356	N377	N398	N419
100%	100%	100%	100%	92%	83%	50%	23%	27%	9%	9%	9%	31%	45%	50%	67%	92%	100%	100%	100%	100%
N1	N22	N43	N64	N85	N106	N127	N148	N169	N190	N211	N231	N252	N273	N294	N315	N336	N357	N378	N399	N420
100%	100%	100%	100%	84%	51%	42%	29%	5%	9%	9%	9%	19%	18%	50%	75%	83%	100%	100%	100%	100%
N2	N23	N44	N65	N86	N107	N128	N149	N170	N191	N212	N232	N253	N274	N295	N316	N337	N358	N379	N400	N421
100%	100%	100%	100%	92%	42%	45%	18%	1%	9%	9%	22%	1%	10%	42%	51%	42%	92%	100%	100%	100%
N3	N24	N45	N66	N87	N108	N129	N150	N171	N192	N213	N233	N254	N275	N296	N317	N338	N359	N380	N401	N422
100%	100%	100%	96%	71%	46%	41%	41%	1%	9%	10%	9%	1%	6%	37%	43%	100%	100%	100%	100%	100%
N4	N25	N46	N67	N88	N109	N130	N151	N172	N193	N214	N234	N255	N276	N297	N318	N339	N360	N381	N402	N423
100%	100%	100%	96%	60%	42%	46%	11%	10%	31%	22%	5%	10%	10%	29%	42%	42%	84%	100%	100%	100%
N5	N26	N47	N68	N89	N110	N131	N152	N173	N194	N215	N235	N256	N277	N298	N319	N340	N361	N382	N403	N424
100%	100%	100%	100%	39%	37%	18%	15%	36%	23%	9%	35%	10%	10%	20%	39%	59%	75%	100%	100%	100%
N6	N27	N48	N69	N90	N111	N132	N153	N174	N195	N216	N236	N257	N278	N299	N320	N341	N362	N383	N404	N425
100%	100%	96%	68%	47%	38%	33%	1%	28%	5%	5%	18%	44%	1%	2%	42%	42%	59%	100%	100%	100%
N7	N28	N49	N70	N91	N112	N133	N154	N175	N196	N217	N237	N258	N279	N300	N321	N342	N363	N384	N405	N426
100%	100%	96%	47%	43%	36%	33%	11%	6%	44%	1%	11%	18%	38%	2%	38%	35%	51%	100%	100%	100%
N8	N29	N50	N71	N92	N113	N134	N155	N176	N197	N218	N238	N259	N280	N301	N322	N343	N364	N385	N406	N427
100%	100%	100%	40%	47%	29%	46%	36%	37%	22%	49%	8%	2%	25%	39%	20%	43%	42%	75%	100%	100%
N9	N30	N51	N72	N93	N114	N135	N156	N177	N198	N219	N239	N260	N281	N302	N323	N344	N365	N386	N407	N428
100%	100%	80%	80%	77%	62%	41%	36%	36%	42%	10%	5%	17%	45%	2%	30%	80%	100%	100%	100%	100%
N10	N31	N52	N73	N94	N115	N136	N157	N178	N199	N220	N240	N261	N282	N303	N324	N345	N366	N387	N408	N429
100%	100%	64%	71%	57%	88%	43%	4%	20%	16%	100%	7%	34%	11%	15%	63%	52%	53%	100%	100%	100%
N11	N32	N53	N74	N95	N116	N137	N158	N179	N200	N220	N241	N262	N283	N304	N325	N346	N367	N388	N409	N430
100%	100%	88%	67%	69%	5%	0%	1%	0%	1%	1%	5%	12%	18%	25%	10%	56%	100%	100%	100%	100%
N12	N33	N54	N75	N96	N117	N138	N159	N180	N201	N221	N242	N263	N284	N305	N326	N347	N368	N389	N410	N431
92%	92%	41%	33%	44%	2%	0%	18%	10%	8%	13%	14%	8%	7%	7%	9%	41%	40%	48%	50%	75%
N13	N34	N55	N76	N97	N118	N139	N160	N181	N202	N222	N243	N264	N285	N306	N327	N348	N369	N390	N411	N432
100%	88%	92%	42%	29%	32%	32%	1%	10%	1%	4%	4%	15%	15%	7%	6%	47%	47%	54%	92%	92%
N14	N35	N56	N77	N98	N119	N140	N161	N182	N203	N223	N244	N265	N286	N307	N328	N349	N370	N391	N412	N433
100%	88%	92%	55%	46%	35%	46%	7%	23%	18%	4%	2%	6%	25%	8%	54%	56%	63%	82%	100%	100%
N15	N36	N57	N78	N99	N120	N141	N162	N183	N204	N224	N245	N266	N287	N308	N329	N350	N371	N392	N413	N434
100%	100%	100%	87%	42%	33%	0%	8%	23%	18%	2%	5%	3%	0%	51%	52%	56%	83%	100%	100%	100%
N16	N37	N58	N79	N100	N121	N142	N163	N184	N205	N225	N246	N267	N288	N309	N330	N351	N372	N393	N414	N435
100%	100%	96%	75%	57%	44%	46%	5%	2%	5%	2%	4%	4%	12%	49%	64%	56%	100%	100%	100%	100%
N17	N38	N59	N80	N101	N122	N143	N164	N185	N206	N226	N247	N268	N289	N310	N331	N352	N373	N394	N415	N436
100%	100%	100%	100%	47%	40%	40%	31%	1%	1%	9%	9%	36%	6%	56%	64%	53%	100%	100%	100%	100%
N18	N39	N60	N81	N102	N123	N144	N165	N186	N207	N227	N248	N269	N290	N311	N332	N353	N374	N395	N416	N437
100%	100%	100%	100%	82%	46%	50%	16%	1%	8%	9%	5%	19%	13%	43%	65%	65%	100%	100%	100%	100%
N19	N40	N61	N82	N103	N124	N145	N166	N187	N208	N228	N249	N270	N291	N312	N333	N354	N375	N396	N417	N438
100%	100%	100%	92%	82%	44%	44%	49%	33%	5%	4%	34%	5%	63%	57%	56%	83%	92%	100%	100%	100%
N20	N41	N62	N83	N104	N125	N146	N167	N188	N209	N229	N250	N271	N292	N313	N334	N355	N376	N397	N418	N439
100%	100%	100%	100%	92%	74%	50%	50%	41%	43%	86%	86%	57%	57%	50%	56%	100%	100%	100%	100%	100%

Optimal Task Assignment in Sensor Networks



RESULTS

Optimal assignment – Run #1

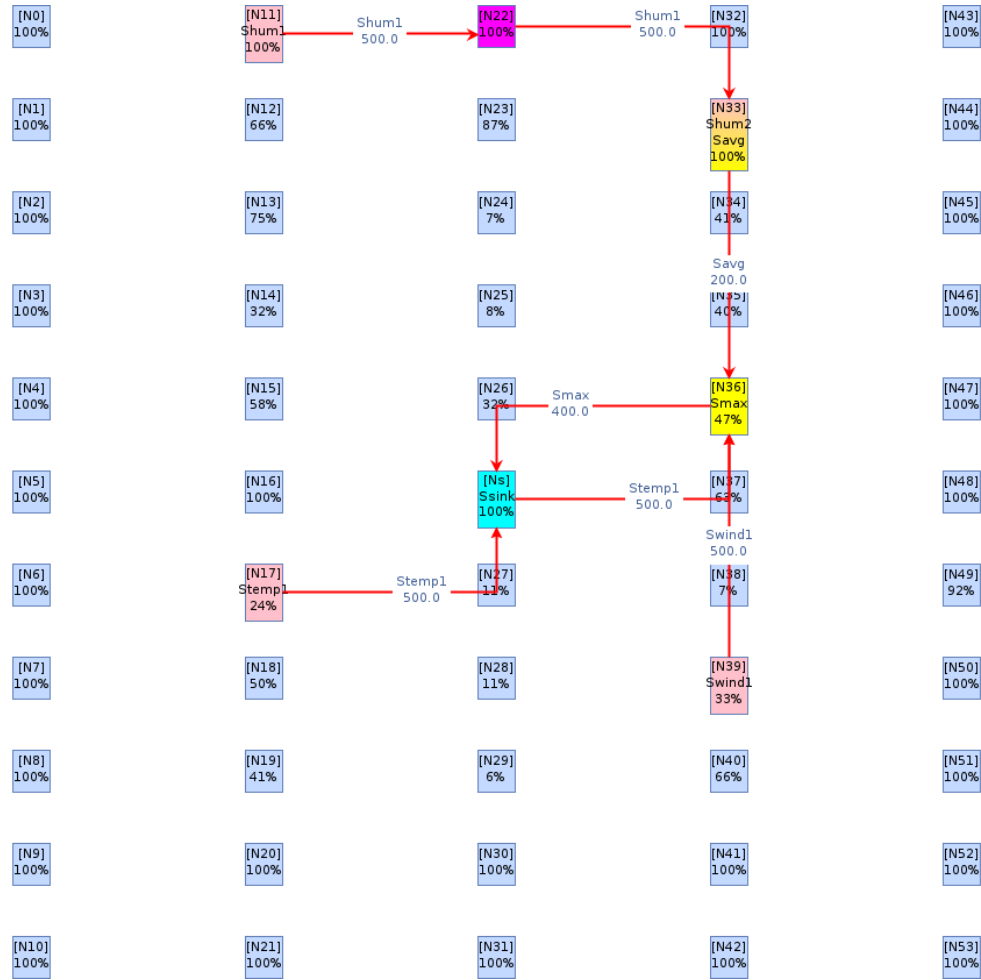


Optimal Task Assignment in Sensor Networks



RESULTS

Optimal assignment – Run #21



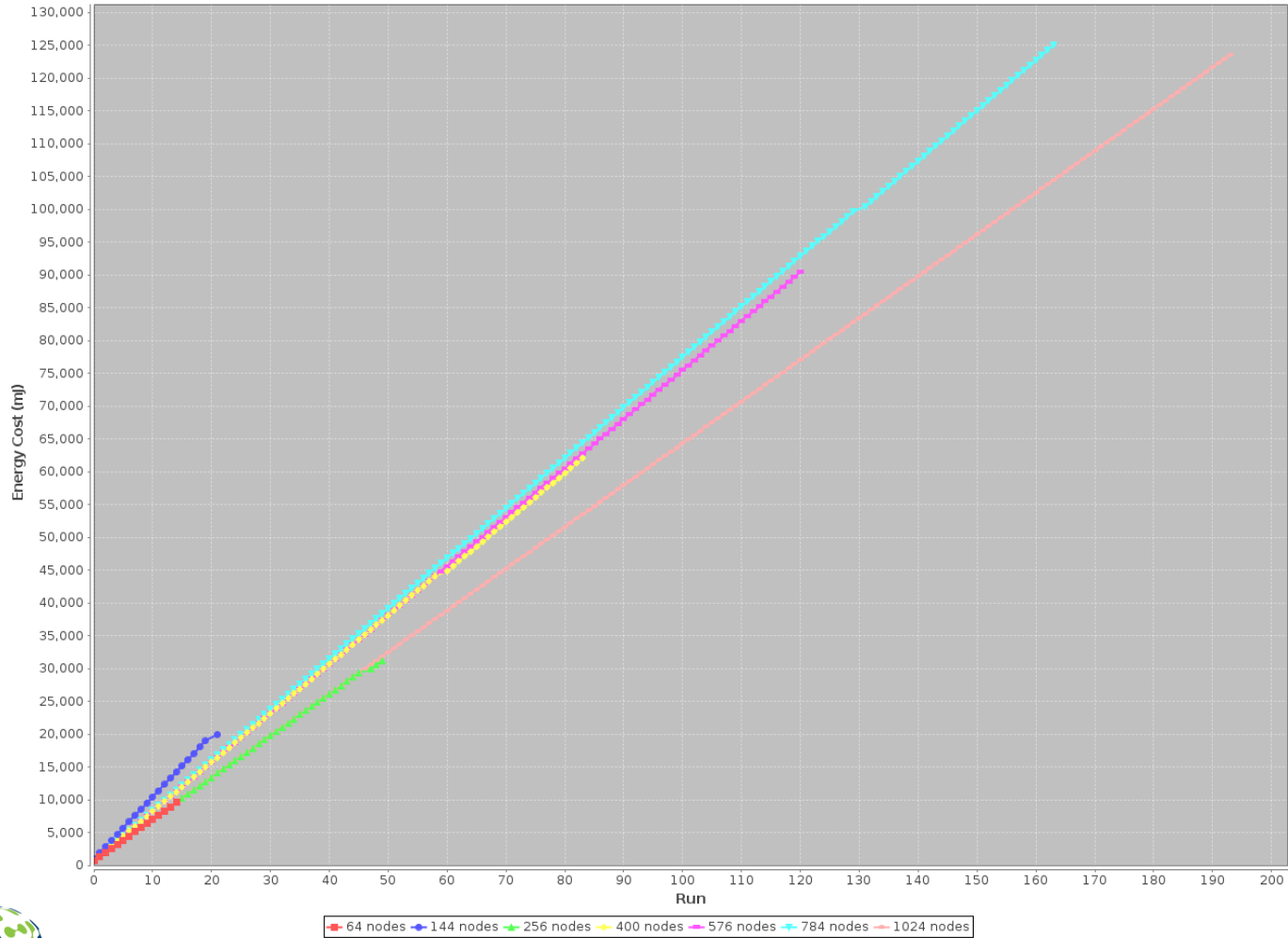
Optimal Task Assignment in Sensor Networks



RESULTS

Mesh network

Per Alg - ILP - Det. Cumulative Communication Energy Cost

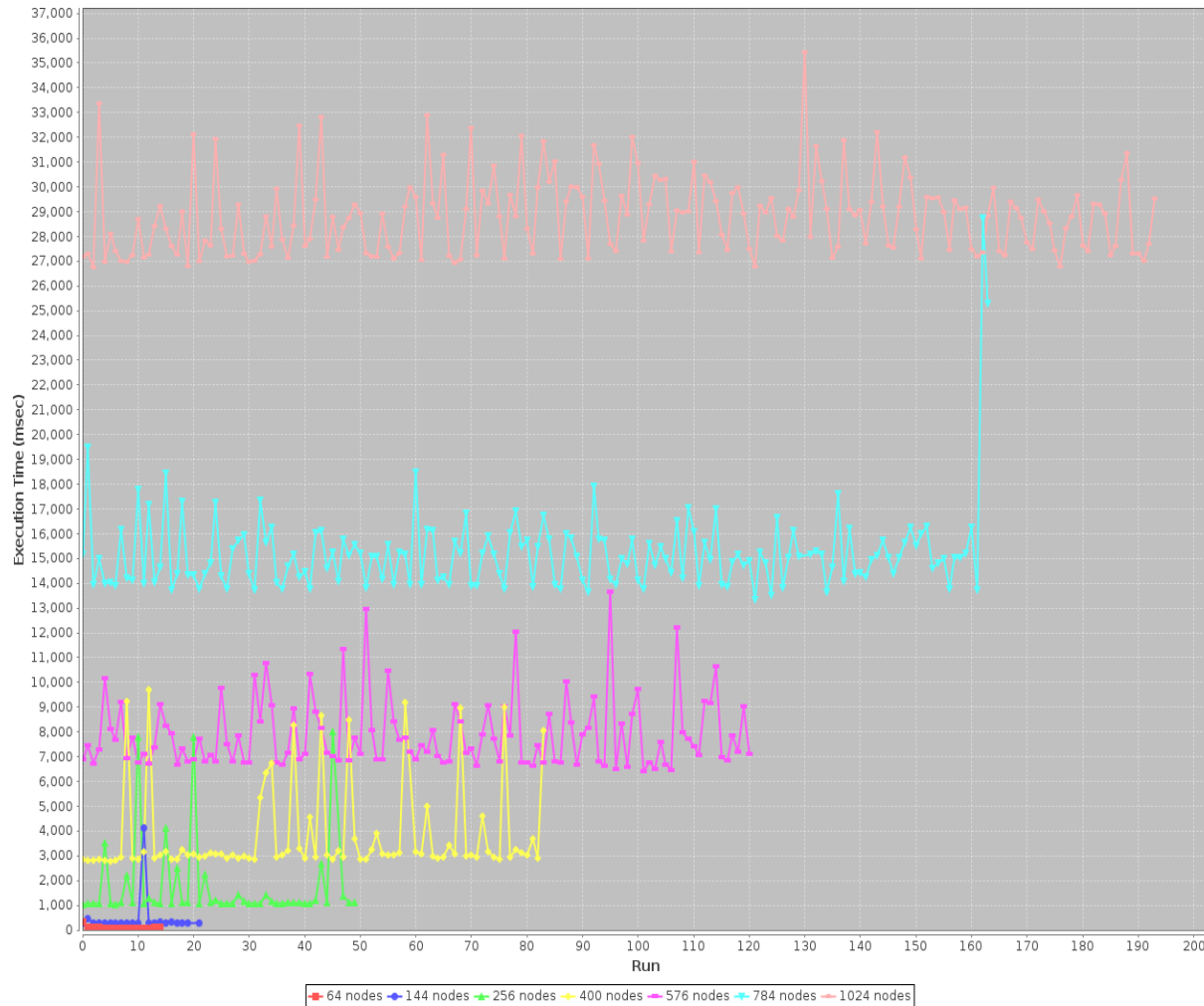


Optimal Task Assignment in Sensor Networks

RESULTS

Mesh network

Per Alg - ILP - Det. Execution Time



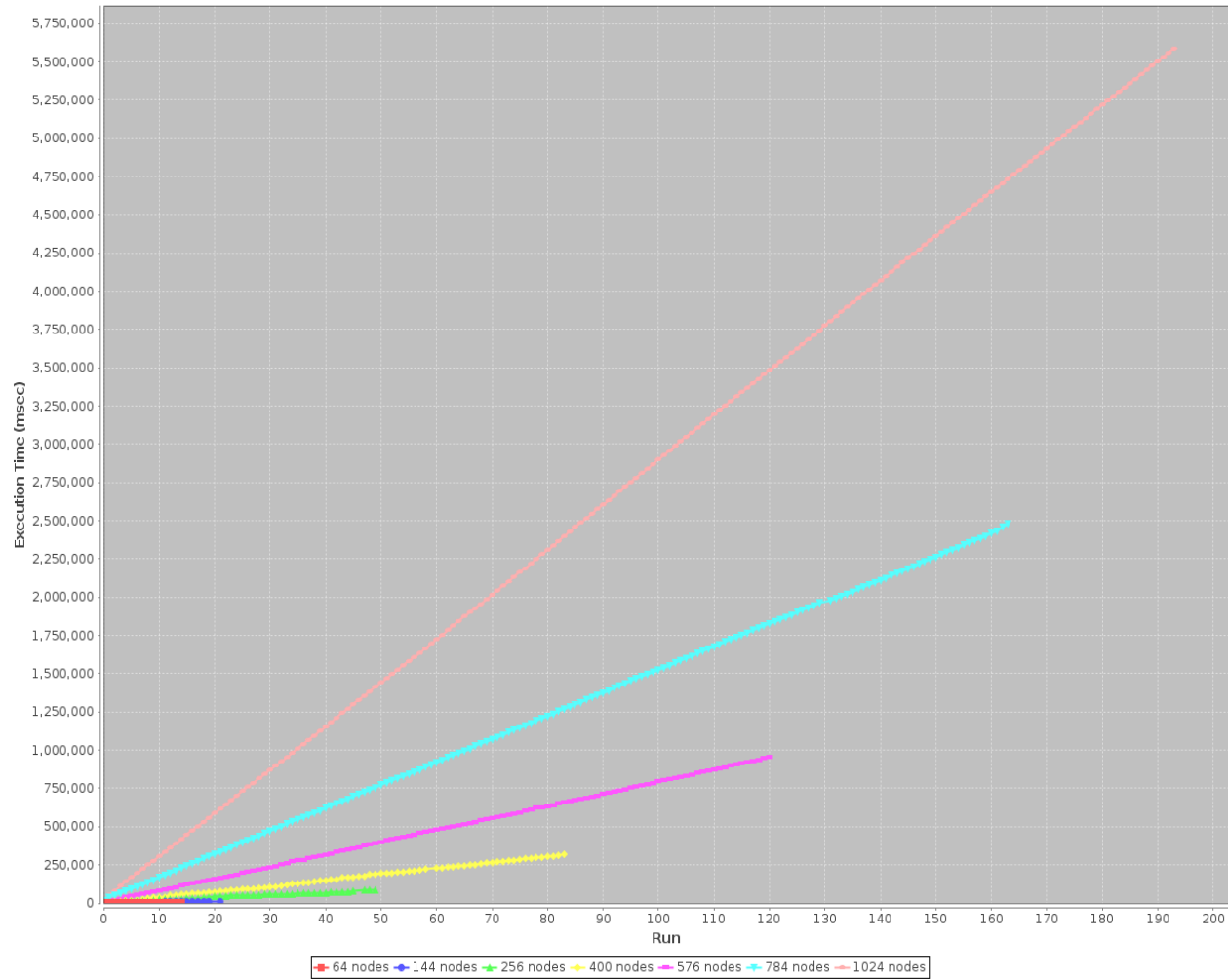
Optimal Task Assignment in Sensor Networks



RESULTS

Mesh network

Per Alg - ILP - Det. Cumulative Execution Time



Optimal Task Assignment in Sensor Networks



FUTURE WORK & EXTENSIONS

- Experimentation with non-optimal solutions that scale
- Maximize the network lifetime instead of minimizing the energy at each step separately
- Model the unreliability of wireless channels
- Insert the concept of *mobility* (Levy Walk model)
- Incremental assignment of tasks



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